# Package 'sgs'

May 6, 2025

Title Sparse-Group SLOPE: Adaptive Bi-Level Selection with FDR Control

Version 0.3.7

Date 2025-05-06

Maintainer Fabio Feser <ff120@ic.ac.uk>

Description Implementation of Sparse-group SLOPE (SGS) (Feser and Evan-

gelou (2023) <doi:10.48550/arXiv.2305.09467>) models. Linear and logistic regression models are supported, both of which can be fit using k-fold cross-validation. Dense and sparse input matrices are supported. In addition, a general Adaptive Three Operator Splitting (ATOS) (Pedregosa and Gidel (2018) <doi:10.48550/arXiv.1804.02339>) implementation is provided. Group SLOPE (gS-

LOPE) (Brzyski et al. (2019) <doi:10.1080/01621459.2017.1411269>) and group-based OS-CAR models (Feser and Evangelou (2024) <doi:10.48550/arXiv.2405.15357>) are also implemented. All models are available with strong screening rules (Feser and Evangelou (2024) <doi:10.48550/arXiv.2405.15357>) for computational speed-up.

**Imports** Matrix, MASS, caret, grDevices, graphics, methods, stats, SLOPE, Rlab, Rcpp (>= 1.0.10)

LinkingTo Rcpp, RcppArmadillo

Suggests SGL, gglasso, glmnet, testthat, knitr, grpSLOPE, rmarkdown

RoxygenNote 7.3.1

License GPL (>= 3)

Encoding UTF-8

URL https://github.com/ff1201/sgs

BugReports https://github.com/ff1201/sgs/issues

VignetteBuilder knitr

NeedsCompilation yes

Author Fabio Feser [aut, cre] (ORCID: <a href="https://orcid.org/0009-0007-3088-9727">https://orcid.org/0009-0007-3088-9727</a>>)

**Repository** CRAN

Date/Publication 2025-05-06 14:20:02 UTC

# Contents

arma_mv	2
arma_sparse	3
as_sgs	3
atos	5
coef.sgs	7
fit_goscar	8
fit_goscar_cv	11
fit_gslope	14
fit_gslope_cv	18
fit_sgo	21
fit_sgo_cv	24
fit_sgs	27
fit_sgs_cv	32
gen_pens	35
gen_toy_data	37
plot.sgs	38
predict.sgs	39
print.sgs	40
scaled_sgs	41
	44

## Index

arma\_mv

Matrix Product in RcppArmadillo.

# Description

Matrix Product in RcppArmadillo.

## Usage

arma\_mv(m, v)

# Arguments

m	numeric matrix
V	numeric vector

## Value

matrix product of m and v

arma\_sparse

#### Description

Matrix Product in RcppArmadillo.

#### Usage

arma\_sparse(m, v)

#### Arguments

m	numeric sparse matrix
v	numeric vector

## Value

matrix product of m and v

as\_sgs

Fits the adaptively scaled SGS model (AS-SGS).

#### Description

Fits an SGS model using the noise estimation procedure, termed adaptively scaled SGS (Algorithm 2 from Feser and Evangelou (2023)). This adaptively estimates  $\lambda$  and then fits the model using the estimated value. It is an alternative approach to cross-validation (fit\_sgs\_cv()). The approach is only compatible with the SGS penalties.

#### Usage

```
as_sgs(
   X,
   y,
   groups,
   type = "linear",
   pen_method = 2,
   alpha = 0.95,
   vFDR = 0.1,
   gFDR = 0.1,
   standardise = "l2",
   intercept = TRUE,
   verbose = FALSE
)
```

#### Arguments

Х		Input matrix of dimensions $n \times p$ . Can be a sparse matrix (using class "sparseMatrix" from the Matrix package).
У		Output vector of dimension $n$ . For type="linear" should be continuous and for type="logistic" should be a binary variable.
g	roups	A grouping structure for the input data. Should take the form of a vector of group indices.
t	уре	The type of regression to perform. Supported values are: "linear" and "logistic".
р	en_method	The type of penalty sequences to use.
		• "1" uses the vMean and gMean SGS sequences.
		• "2" uses the vMax and gMax SGS sequences.
а	lpha	The value of $\alpha$ , which defines the convex balance between SLOPE and gSLOPE. Must be between 0 and 1.
v	FDR	Defines the desired variable false discovery rate (FDR) level, which determines the shape of the variable penalties. Must be between 0 and 1.
g	FDR	Defines the desired group false discovery rate (FDR) level, which determines the shape of the group penalties. Must be between 0 and 1.
s	tandardise	Type of standardisation to perform on X:
		• "12" standardises the input data to have $\ell_2$ norms of one.
		• "11" standardises the input data to have $\ell_1$ norms of one.
		• "sd" standardises the input data to have standard deviation of one.
		• "none" no standardisation applied.
i	ntercept	Logical flag for whether to fit an intercept.
v	erbose	Logical flag for whether to print fitting information.

#### Value

An object of type "sgs" containing model fit information (see fit\_sgs()).

#### References

Feser, F., Evangelou, M. (2023). *Sparse-group SLOPE: adaptive bi-level selection with FDR-control*, https://arxiv.org/abs/2305.09467

## See Also

#### scaled\_sgs()

Other model-selection: fit\_goscar\_cv(), fit\_gslope\_cv(), fit\_sgo\_cv(), fit\_sgs\_cv(), scaled\_sgs()

Other SGS-methods: coef.sgs(), fit\_sgo(), fit\_sgo\_cv(), fit\_sgs(), fit\_sgs\_cv(), plot.sgs(), predict.sgs(), print.sgs(), scaled\_sgs()

## atos

## Description

Function for fitting adaptive three operator splitting (ATOS) with general convex penalties. Supports both linear and logistic regression, both with dense and sparse matrix implementations.

#### Usage

```
atos(
 Χ,
 у,
  type = "linear",
 prox_1,
  prox_2,
 pen_prox_1 = 0.5,
  pen_prox_2 = 0.5,
 max_iter = 5000,
 backtracking = 0.7,
 max_iter_backtracking = 100,
  tol = 1e-05,
  prox_1_opts = NULL,
  prox_2_opts = NULL,
  standardise = "12",
  intercept = TRUE,
  x0 = NULL,
  u = NULL,
  verbose = FALSE
)
```

Х	Input matrix of dimensions $n \times p$ . Can be a sparse matrix (using class "sparseMatrix" from the Matrix package)
У	Output vector of dimension $n$ . For type="linear" needs to be continuous and for type="logistic" needs to be a binary variable.
type	The type of regression to perform. Supported values are: "linear" and "logistic".
prox_1	The proximal operator for the first function, $h(x)$ .
prox_2	The proximal operator for the second function, $g(x)$ .
pen_prox_1	The penalty for the first proximal operator. For the lasso, this would be the sparsity parameter, $\lambda$ . If operator does not include a penalty, set to 1.
pen_prox_2	The penalty for the second proximal operator.
max_iter	Maximum number of ATOS iterations to perform.
backtracking	The backtracking parameter, $\tau$ , as defined in Pedregosa and Gidel (2018).

max_	_iter_	backtr	acking
------	--------	--------	--------

	Maximum number of backtracking line search iterations to perform per global iteration.
tol	Convergence tolerance for the stopping criteria.
prox_1_opts	Optional argument for first proximal operator. For the group lasso, this would be the group IDs. Note: this must be inserted as a list.
prox_2_opts	Optional argument for second proximal operator.
standardise	Type of standardisation to perform on X:
	• "12" standardises the input data to have $\ell_2$ norms of one.
	• "11" standardises the input data to have $\ell_1$ norms of one.
	• "sd" standardises the input data to have standard deviation of one.
	<ul> <li>"none" no standardisation applied.</li> </ul>
intercept	Logical flag for whether to fit an intercept.
x0	Optional initial vector for $x_0$ .
u	Optional initial vector for <i>u</i> .
verbose	Logical flag for whether to print fitting information.

## Details

atos() solves convex minimization problems of the form

$$f(x) + g(x) + h(x),$$

where f is convex and differentiable with  $L_f$ -Lipschitz gradient, and g and h are both convex. The algorithm is not symmetrical, but usually the difference between variations are only small numerical values, which are filtered out. However, both variations should be checked regardless, by looking at x and u. An example for the sparse-group lasso (SGL) is given.

#### Value

An object of class "atos" containing:

beta	The fitted values from the regression. Taken to be the more stable fit between $x$ and $u$ , which is usually the former.
x	The solution to the original problem (see Pedregosa and Gidel (2018)).
u	The solution to the dual problem (see Pedregosa and Gidel (2018)).
Z	The updated values from applying the first proximal operator (see Pedregosa and Gidel (2018)).
type	Indicates which type of regression was performed.
success	Logical flag indicating whether ATOS converged, according to tol.
num_it	Number of iterations performed. If convergence is not reached, this will be max_iter.
certificate	Final value of convergence criteria.
intercept	Logical flag indicating whether an intercept was fit.

#### coef.sgs

#### References

Pedregosa, F., Gidel, G. (2018). *Adaptive Three Operator Splitting*, https://proceedings.mlr. press/v80/pedregosa18a.html

coef.sgs	Extracts coefficients for	r one of the	following	object types:	"sgs",
	"sgs_cv", "gslope", "g	gslope_cv".			

#### Description

Print the coefficients using model fitted with one of the following functions: fit\_sgs(), fit\_sgs\_cv(), fit\_gslope(), fit\_gslope\_cv(), fit\_sgo(), fit\_sgo\_cv(), fit\_goscar\_cv(), fit\_goscar\_cv(). The predictions are calculated for each "lambda" value in the path.

#### Usage

```
## S3 method for class 'sgs'
coef(object, ...)
```

### Arguments

object	Object of one of the following classes: "sgs", "sgs_cv", "gslope", "gslope_cv".
	further arguments passed to stats function.

#### Value

The fitted coefficients

## See Also

```
fit_sgs(), fit_sgs_cv(), fit_gslope(), fit_gslope_cv()
Other SGS-methods: as_sgs(), fit_sgo(), fit_sgo_cv(), fit_sgs(), fit_sgs_cv(), plot.sgs(),
predict.sgs(), print.sgs(), scaled_sgs()
Other gSLOPE-methods: fit_goscar(), fit_goscar_cv(), fit_gslope(), fit_gslope_cv(),
plot.sgs(), predict.sgs(), print.sgs()
```

#### Examples

```
# specify a grouping structure
groups = c(1,1,1,2,2,3,3,3,4,4)
# generate data
data = gen_toy_data(p=10, n=5, groups = groups, seed_id=3,group_sparsity=1)
# run SGS
model = fit_sgs(X = data$X, y = data$y, groups = groups, type="linear", lambda = 1, alpha=0.95,
vFDR=0.1, gFDR=0.1, standardise = "l2", intercept = TRUE, verbose=FALSE)
# use predict function
model_coef = coef(model)
```

fit\_goscar

## Description

Group OSCAR (gOSCAR) main fitting function. Supports both linear and logistic regression, both with dense and sparse matrix implementations.

## Usage

```
fit_goscar(
 Χ,
 у,
 groups,
 type = "linear",
lambda = "path",
 path_length = 20,
 min_frac = 0.05,
 max_iter = 5000,
 backtracking = 0.7,
 max_iter_backtracking = 100,
  tol = 1e-05,
  standardise = "12",
  intercept = TRUE,
  screen = TRUE,
 verbose = FALSE,
 w_weights = NULL,
 warm_start = NULL
)
```

Х	Input matrix of dimensions $n \times p$ . Can be a sparse matrix (using class "sparseMatrix" from the Matrix package).
У	Output vector of dimension $n$ . For type="linear" should be continuous and for type="logistic" should be a binary variable.
groups	A grouping structure for the input data. Should take the form of a vector of group indices.
type	The type of regression to perform. Supported values are: "linear" and "logistic".
lambda	The regularisation parameter. Defines the level of sparsity in the model. A higher value leads to sparser models:
	• "path" computes a path of regularisation parameters of length "path_length". The path will begin just above the value at which the first predictor enters the model and will terminate at the value determined by min_frac.

	• User-specified single value or sequence. Internal scaling is applied based on the type of standardisation. The returned "lambda" value will be the original unscaled value(s).
path_length	The number of $\lambda$ values to fit the model for. If "lambda" is user-specified, this is ignored.
min_frac	Smallest value of $\lambda$ as a fraction of the maximum value. That is, the final $\lambda$ will be "min_frac" of the first $\lambda$ value.
max_iter	Maximum number of ATOS iterations to perform.
backtracking	The backtracking parameter, $\tau$ , as defined in Pedregosa and Gidel (2018).
<pre>max_iter_backt</pre>	
	Maximum number of backtracking line search iterations to perform per global iteration.
tol	Convergence tolerance for the stopping criteria.
standardise	Type of standardisation to perform on X:
	• "12" standardises the input data to have $\ell_2$ norms of one. When using this "lambda" is scaled internally by $1/\sqrt{n}$ .
	• "11" standardises the input data to have $\ell_1$ norms of one. When using this "lambda" is scaled internally by $1/n$ .
	• "sd" standardises the input data to have standard deviation of one.
	• "none" no standardisation applied.
intercept	Logical flag for whether to fit an intercept.
screen	Logical flag for whether to apply screening rules (see Feser and Evangelou (2024)). Screening discards irrelevant groups before fitting, greatly improving speed.
verbose	Logical flag for whether to print fitting information.
w_weights	Optional vector for the group penalty weights. Overrides the OSCAR penalties when specified. When entering custom weights, these are multiplied internally by $\lambda$ . To void this behaviour, set $\lambda = 1$ .
warm_start	Optional list for implementing warm starts. These values are used as initial values in the fitting algorithm. Need to supply "x" and "u" in the form "list(warm_x, warm_u)". Not recommended for use with a path or CV fit as start from the null model by design.

## Details

fit\_goscar() fits a gOSCAR model (Feser and Evangelou (2024)) using adaptive three operator splitting (ATOS). gOSCAR uses the same model set-up as for gSLOPE, but with different weights (see Bao et al. (2020) and Feser and Evangelou (2024)). The penalties are given by (for a group g with m groups):

$$w_g = \sigma_1 + \sigma_3(m - g),$$

where

$$\sigma_1 = d_i \| X^{\mathsf{T}} y \|_{\infty}, \ \sigma_3 = \sigma_1 / m.$$

## Value

A list containing:

beta	The fitted values from the regression. Taken to be the more stable fit between $x$ and $z$ , which is usually the former. A filter is applied to remove very small values, where ATOS has not been able to shrink exactly to zero. Check this against $x$ and $z$ .
group_effects	The group values from the regression. Taken by applying the $\ell_2$ norm within each group on beta.
selected_var	A list containing the indicies of the active/selected variables for each "lambda" value. Index 1 corresponds to the first column in X.
selected_grp	A list containing the indicies of the active/selected groups for each "lambda" value. Index 1 corresponds to the first group in the groups vector. You can see the group order by running unique(groups).
num_it	Number of iterations performed. If convergence is not reached, this will be max_iter.
success	Logical flag indicating whether ATOS converged, according to tol.
certificate	Final value of convergence criteria.
x	The solution to the original problem (see Pedregosa and Gidel (2018)).
u	The solution to the dual problem (see Pedregosa and Gidel (2018)).
Z	The updated values from applying the first proximal operator (see Pedregosa and Gidel (2018)).
screen_set	List of groups that were kept after screening step for each "lambda" value. (corresponds to $S$ in Feser and Evangelou (2024)).
epsilon_set	List of groups that were used for fitting after screening for each "lambda" value. (corresponds to $\mathcal{E}$ in Feser and Evangelou (2024)).
kkt_violations	List of groups that violated the KKT conditions each "lambda" value. (corresponds to $\mathcal{K}$ in Feser and Evangelou (2024)).
pen_gslope	Vector of the group penalty sequence.
screen	Logical flag indicating whether screening was applied.
type	Indicates which type of regression was performed.
intercept	Logical flag indicating whether an intercept was fit.
standardise	Type of standardisation used.
lambda	Value(s) of $\lambda$ used to fit the model.

#### References

Bao, R., Gu B., Huang, H. (2020). *Fast OSCAR and OWL Regression via Safe Screening Rules*, https://proceedings.mlr.press/v119/bao20b

Feser, F., Evangelou, M. (2024). *Strong screening rules for group-based SLOPE models*, https://arxiv.org/abs/2405.15357

Pedregosa, F., Gidel, G. (2018). *Adaptive Three Operator Splitting*, https://proceedings.mlr.press/v80/pedregosa18a.html

#### fit\_goscar\_cv

#### See Also

```
Other gSLOPE-methods: coef.sgs(), fit_goscar_cv(), fit_gslope(), fit_gslope_cv(), plot.sgs(),
predict.sgs(), print.sgs()
```

#### Examples

```
# specify a grouping structure
groups = c(1,1,1,2,2,3,3,3,4,4)
# generate data
data = gen_toy_data(p=10, n=5, groups = groups, seed_id=3,group_sparsity=1)
# run gOSCAR
model = fit_goscar(X = data$X, y = data$y, groups = groups, type="linear", path_length = 5,
standardise = "12", intercept = TRUE, verbose=FALSE)
```

fit\_goscar\_cv

Fit a gOSCAR model using k-fold cross-validation.

#### Description

Function to fit a pathwise solution of group OSCAR (gOSCAR) models using k-fold cross-validation. Supports both linear and logistic regression, both with dense and sparse matrix implementations.

#### Usage

```
fit_goscar_cv(
 Х,
 у,
  groups,
  type = "linear",
  lambda = "path",
 path_length = 20,
 min_frac = 0.05,
 nfolds = 10,
 backtracking = 0.7,
 max_iter = 5000,
 max_iter_backtracking = 100,
  tol = 1e-05,
  standardise = "12",
  intercept = TRUE,
  error_criteria = "mse",
  screen = TRUE,
  verbose = FALSE,
 w_weights = NULL,
  warm_start = NULL
)
```

X	Input matrix of dimensions $n \times p$ . Can be a sparse matrix (using class "sparseMatrix" from the Matrix package).
У	Output vector of dimension $n$ . For type="linear" should be continuous and for type="logistic" should be a binary variable.
groups	A grouping structure for the input data. Should take the form of a vector of group indices.
type	The type of regression to perform. Supported values are: "linear" and "logistic".
lambda	The regularisation parameter. Defines the level of sparsity in the model. A higher value leads to sparser models:
	<ul> <li>"path" computes a path of regularisation parameters of length "path_length". The path will begin just above the value at which the first predictor enters the model and will terminate at the value determined by "min_frac".</li> <li>User-specified single value or sequence. Internal scaling is applied based on the type of standardisation. The returned "lambda" value will be the original unscaled value(s).</li> </ul>
path_length	The number of $\lambda$ values to fit the model for. If "lambda" is user-specified, this is ignored.
min_frac	Smallest value of $\lambda$ as a fraction of the maximum value. That is, the final $\lambda$ will be "min_frac" of the first $\lambda$ value.
nfolds	The number of folds to use in cross-validation.
backtracking	The backtracking parameter, $\tau$ , as defined in Pedregosa and Gidel (2018).
max_iter	Maximum number of ATOS iterations to perform.
<pre>max_iter_backtr</pre>	-
	Maximum number of backtracking line search iterations to perform per global iteration.
tol	Convergence tolerance for the stopping criteria.
standardise	Type of standardisation to perform on X:
	• "12" standardises the input data to have $\ell_2$ norms of one.
	• "11" standardises the input data to have $\ell_1$ norms of one.
	<ul> <li>"sd" standardises the input data to have standard deviation of one.</li> <li>"none" no standardisation applied.</li> </ul>
intercept	Logical flag for whether to fit an intercept.
error_criteria	The criteria used to discriminate between models along the path. Supported values are: "mse" (mean squared error) and "mae" (mean absolute error).
screen	Logical flag for whether to apply screening rules (see Feser and Evangelou (2024)). Screening discards irrelevant groups before fitting, greatly improving speed.
verbose	Logical flag for whether to print fitting information.
w_weights	Optional vector for the group penalty weights. Overrides the OSCAR penalties when specified. When entering custom weights, these are multiplied internally by $\lambda$ . To void this behaviour, set $\lambda = 1$ .

#### fit\_goscar\_cv

warm_start	Optional list for implementing warm starts. These values are used as initial val-
	ues in the fitting algorithm. Need to supply "x" and "u" in the form "list(warm_x,
	warm_u)". Not recommended for use with a path or CV fit as start from the null
	model by design.

## Details

Fits gOSCAR models under a pathwise solution using adaptive three operator splitting (ATOS), picking the 1se model as optimum. Warm starts are implemented.

#### Value

A list containing:

errors	A table containing fitting information about the models on the path.
all_models	Fitting information for all models fit on the path, which is a "gslope" object type.
fit	The 1se chosen model, which is a "gslope" object type.
best_lambda	The value of $\lambda$ which generated the chosen model.
best_lambda_id	The path index for the chosen model.

#### References

Bao, R., Gu B., Huang, H. (2020). *Fast OSCAR and OWL Regression via Safe Screening Rules*, https://proceedings.mlr.press/v119/bao20b

Feser, F., Evangelou, M. (2024). *Strong screening rules for group-based SLOPE models*, https://arxiv.org/abs/2405.15357

## See Also

fit\_goscar()

Other gSLOPE-methods: coef.sgs(), fit\_goscar(), fit\_gslope(), fit\_gslope\_cv(), plot.sgs(), predict.sgs(), print.sgs()

Other model-selection: as\_sgs(), fit\_gslope\_cv(), fit\_sgo\_cv(), fit\_sgs\_cv(), scaled\_sgs()

#### Examples

```
# specify a grouping structure
groups = c(1,1,1,2,2,3,3,3,4,4)
# generate data
data = gen_toy_data(p=10, n=5, groups = groups, seed_id=3,group_sparsity=1)
# run gOSCAR with cross-validation
cv_model = fit_goscar_cv(X = data$X, y = data$y, groups=groups, type = "linear", path_length = 5,
nfolds=5, min_frac = 0.05, standardise="l2",intercept=TRUE,verbose=TRUE)
```

fit\_gslope

#### Description

Group SLOPE (gSLOPE) main fitting function. Supports both linear and logistic regression, both with dense and sparse matrix implementations.

#### Usage

```
fit_gslope(
 Χ,
 у,
  groups,
  type = "linear",
  lambda = "path",
  path_length = 20,
 min_frac = 0.05,
 gFDR = 0.1,
 pen_method = 1,
 max_iter = 5000,
 backtracking = 0.7,
 max_iter_backtracking = 100,
  tol = 1e-05,
  standardise = "12",
  intercept = TRUE,
  screen = TRUE,
  verbose = FALSE,
 w_weights = NULL,
 warm_start = NULL
)
```

Х	Input matrix of dimensions $n \times p$ . Can be a sparse matrix (using class "sparseMatrix" from the Matrix package).
У	Output vector of dimension $n$ . For type="linear" should be continuous and for type="logistic" should be a binary variable.
groups	A grouping structure for the input data. Should take the form of a vector of group indices.
type	The type of regression to perform. Supported values are: "linear" and "logistic".
lambda	The regularisation parameter. Defines the level of sparsity in the model. A higher value leads to sparser models:
	• "path" computes a path of regularisation parameters of length "path_length". The path will begin just above the value at which the first predictor enters the model and will terminate at the value determined by "min_frac".

	• User-specified single value or sequence. Internal scaling is applied based on the type of standardisation. The returned "lambda" value will be the original unscaled value(s).
path_length	The number of $\lambda$ values to fit the model for. If "lambda" is user-specified, this is ignored.
min_frac	Smallest value of $\lambda$ as a fraction of the maximum value. That is, the final $\lambda$ will be "min_frac" of the first $\lambda$ value.
gFDR	Defines the desired group false discovery rate (FDR) level, which determines the shape of the group penalties. Must be between 0 and 1.
pen_method	The type of penalty sequences to use (see Brzyski et al. (2019)):
	• "1" uses the gMean gSLOPE sequence.
	• "2" uses the gMax gSLOPE sequence.
<pre>max_iter</pre>	Maximum number of ATOS iterations to perform.
backtracking	The backtracking parameter, $\tau$ , as defined in Pedregosa and Gidel (2018).
<pre>max_iter_backt</pre>	-
	Maximum number of backtracking line search iterations to perform per global iteration.
tol	Convergence tolerance for the stopping criteria.
standardise	Type of standardisation to perform on X:
	• "12" standardises the input data to have $\ell_2$ norms of one. When using this "lambda" is scaled internally by $1/\sqrt{n}$ .
	• "11" standardises the input data to have $\ell_1$ norms of one. When using this "lambda" is scaled internally by $1/n$ .
	• "sd" standardises the input data to have standard deviation of one.
	"none" no standardisation applied.
intercept	Logical flag for whether to fit an intercept.
screen	Logical flag for whether to apply screening rules (see Feser and Evangelou (2024)). Screening discards irrelevant groups before fitting, greatly improving speed.
verbose	Logical flag for whether to print fitting information.
w_weights	Optional vector for the group penalty weights. Overrides the penalties from pen_method if specified. When entering custom weights, these are multiplied internally by $\lambda$ . To void this behaviour, set $\lambda = 1$ .
warm_start	Optional list for implementing warm starts. These values are used as initial values in the fitting algorithm. Need to supply "x" and "u" in the form "list(warm_x, warm_u)". Not recommended for use with a path or CV fit as start from the null model by design.

## Details

fit\_gslope() fits a gSLOPE model (Brzyski et al. (2019)) using adaptive three operator splitting (ATOS). gSLOPE is a sparse-group method, so that it selects both variables and groups. Unlike

group selection approaches, not every variable within a group is set as active. It solves the convex optimisation problem given by

$$\frac{1}{2n}f(b;y,\mathbf{X}) + \lambda \sum_{g=1}^m w_g \sqrt{p_g} \|b^{(g)}\|_2,$$

where the penalty sequences are sorted and  $f(\cdot)$  is the loss function. In the case of the linear model, the loss function is given by the mean-squared error loss:

$$f(b; y, \mathbf{X}) = ||y - \mathbf{X}b||_2^2$$

In the logistic model, the loss function is given by

$$f(b; y, \mathbf{X}) = -1/n \log(\mathcal{L}(b; y, \mathbf{X})).$$

where the log-likelihood is given by

$$\mathcal{L}(b; y, \mathbf{X}) = \sum_{i=1}^{n} \left\{ y_i b^{\mathsf{T}} x_i - \log(1 + \exp(b^{\mathsf{T}} x_i)) \right\}.$$

The penalty parameters in gSLOPE are sorted so that the largest group effects are matched with the largest penalties, to reduce the group FDR. The gMean sequence (pen\_method=1) is given by

$$w_i^{\text{mean}} = \overline{F}_{\chi_{p_j}}^{-1}(1 - q_g i/m), \ i = 1, \dots, m, \text{where } \overline{F}_{\chi_{p_j}}(x) := \frac{1}{m} \sum_{j=1}^m F_{\chi_{p_j}}(\sqrt{p_j}x),$$

where  $F_{\chi_{p_j}}$  is the cumulative distribution function of a  $\chi$  distribution with  $p_j$  degrees of freedom. The gMax sequence (pen\_method=2) is given by

$$w_i^{\max} = \max_{j=1,...,m} \left\{ \frac{1}{\sqrt{p_j}} F_{\chi_{p_j}}^{-1} \left( 1 - \frac{q_g i}{m} \right) \right\},$$

where  $F_{\chi_{p_j}}$  is the cumulative distribution function of a  $\chi$  distribution with  $p_j$  degrees of freedom.

#### Value

A list containing:

beta	The fitted values from the regression. Taken to be the more stable fit between $x$ and $z$ , which is usually the former. A filter is applied to remove very small values, where ATOS has not been able to shrink exactly to zero. Check this against $x$ and $z$ .
group_effects	The group values from the regression. Taken by applying the $\ell_2$ norm within each group on beta.
selected_var	A list containing the indicies of the active/selected variables for each "lambda" value. Index 1 corresponds to the first column in X.
selected_grp	A list containing the indicies of the active/selected groups for each "lambda" value. Index 1 corresponds to the first group in the groups vector. You can see the group order by running unique(groups).

fit	gsl	0	pe

num_it	Number of iterations performed. If convergence is not reached, this will be max_iter.
success	Logical flag indicating whether ATOS converged, according to tol.
certificate	Final value of convergence criteria.
х	The solution to the original problem (see Pedregosa and Gidel (2018)).
u	The solution to the dual problem (see Pedregosa and Gidel (2018)).
Z	The updated values from applying the first proximal operator (see Pedregosa and Gidel (2018)).
screen_set	List of groups that were kept after screening step for each "lambda" value. (corresponds to $S$ in Feser and Evangelou (2024)).
epsilon_set	List of groups that were used for fitting after screening for each "lambda" value. (corresponds to $\mathcal{E}$ in Feser and Evangelou (2024)).
kkt_violations	List of groups that violated the KKT conditions each "lambda" value. (corresponds to $\mathcal{K}$ in Feser and Evangelou (2024)).
pen_gslope	Vector of the group penalty sequence.
screen	Logical flag indicating whether screening was applied.
type	Indicates which type of regression was performed.
intercept	Logical flag indicating whether an intercept was fit.
standardise	Type of standardisation used.
lambda	Value(s) of $\lambda$ used to fit the model.

#### References

Brzyski, D., Gossmann, A., Su, W., Bodgan, M. (2019). *Group SLOPE – Adaptive Selection of Groups of Predictors*, https://www.tandfonline.com/doi/full/10.1080/01621459.2017. 1411269

Feser, F., Evangelou, M. (2024). *Strong screening rules for group-based SLOPE models*, https://arxiv.org/abs/2405.15357

Pedregosa, F., Gidel, G. (2018). *Adaptive Three Operator Splitting*, https://proceedings.mlr.press/v80/pedregosa18a.html

## See Also

Other gSLOPE-methods: coef.sgs(), fit\_goscar(), fit\_goscar\_cv(), fit\_gslope\_cv(), plot.sgs(), predict.sgs(), print.sgs()

## Examples

```
# specify a grouping structure
groups = c(1,1,1,2,2,3,3,3,4,4)
# generate data
data = gen_toy_data(p=10, n=5, groups = groups, seed_id=3,group_sparsity=1)
# run gSLOPE
model = fit_gslope(X = data$X, y = data$y, groups = groups, type="linear", path_length = 5,
gFDR=0.1, standardise = "12", intercept = TRUE, verbose=FALSE)
```

```
fit_gslope_cv
```

#### Description

Function to fit a pathwise solution of group SLOPE (gSLOPE) models using k-fold cross-validation. Supports both linear and logistic regression, both with dense and sparse matrix implementations.

#### Usage

```
fit_gslope_cv(
 Х,
 у,
  groups,
  type = "linear",
  lambda = "path",
 path_length = 20,
 min_frac = 0.05,
 nfolds = 10,
  gFDR = 0.1,
 pen_method = 1,
 backtracking = 0.7,
 max_iter = 5000,
 max_iter_backtracking = 100,
  tol = 1e-05,
  standardise = "12",
  intercept = TRUE,
 error_criteria = "mse",
  screen = TRUE,
 verbose = FALSE,
 w_weights = NULL,
 warm_start = NULL
)
```

Х	Input matrix of dimensions $n \times p$ . Can be a sparse matrix (using class "sparseMatrix" from the Matrix package).
У	Output vector of dimension $n$ . For type="linear" should be continuous and for type="logistic" should be a binary variable.
groups	A grouping structure for the input data. Should take the form of a vector of group indices.
type	The type of regression to perform. Supported values are: "linear" and "logistic".
lambda	The regularisation parameter. Defines the level of sparsity in the model. A higher value leads to sparser models:

	<ul> <li>"path" computes a path of regularisation parameters of length "path_length". The path will begin just above the value at which the first predictor enters the model and will terminate at the value determined by "min_frac".</li> <li>User-specified single value or sequence. Internal scaling is applied based on the type of standardisation. The returned "lambda" value will be the original unscaled value(s).</li> </ul>
path_length	The number of $\lambda$ values to fit the model for. If "lambda" is user-specified, this is ignored.
min_frac	Smallest value of $\lambda$ as a fraction of the maximum value. That is, the final $\lambda$ will be "min_frac" of the first $\lambda$ value.
nfolds	The number of folds to use in cross-validation.
gFDR	Defines the desired group false discovery rate (FDR) level, which determines the shape of the penalties. Must be between 0 and 1.
pen_method	The type of penalty sequences to use (see Brzyski et al. (2019)):
	• "1" uses the gMean gSLOPE sequence.
	• "2" uses the gMax gSLOPE sequence.
backtracking	The backtracking parameter, $\tau$ , as defined in Pedregosa and Gidel (2018).
<pre>max_iter</pre>	Maximum number of ATOS iterations to perform.
<pre>max_iter_backtr</pre>	-
	Maximum number of backtracking line search iterations to perform per global iteration.
tol	Convergence tolerance for the stopping criteria.
standardise	Type of standardisation to perform on X:
	• "12" standardises the input data to have $\ell_2$ norms of one.
	• "11" standardises the input data to have $\ell_1$ norms of one.
	• "sd" standardises the input data to have standard deviation of one.
_	• "none" no standardisation applied.
intercept	Logical flag for whether to fit an intercept.
error_criteria	The criteria used to discriminate between models along the path. Supported values are: "mse" (mean squared error) and "mae" (mean absolute error).
screen	Logical flag for whether to apply screening rules (see Feser and Evangelou (2024)). Screening discards irrelevant groups before fitting, greatly improving speed.
verbose	Logical flag for whether to print fitting information.
w_weights	Optional vector for the group penalty weights. Overrides the penalties from pen_method if specified. When entering custom weights, these are multiplied internally by $\lambda$ . To void this behaviour, set $\lambda = 1$ .
warm_start	Optional list for implementing warm starts. These values are used as initial values in the fitting algorithm. Need to supply "x" and "u" in the form "list(warm_x, warm_u)". Not recommended for use with a path or CV fit as start from the null model by design.

#### Details

Fits gSLOPE models under a pathwise solution using adaptive three operator splitting (ATOS), picking the 1se model as optimum. Warm starts are implemented.

## Value

A list containing:

errors	A table containing fitting information about the models on the path.
all_models	Fitting information for all models fit on the path, which is a "gslope" object type.
fit	The 1se chosen model, which is a "gslope" object type.
best_lambda	The value of $\lambda$ which generated the chosen model.
best_lambda_id	The path index for the chosen model.

## References

Brzyski, D., Gossmann, A., Su, W., Bodgan, M. (2019). *Group SLOPE – Adaptive Selection of Groups of Predictors*, https://www.tandfonline.com/doi/full/10.1080/01621459.2017. 1411269

Feser, F., Evangelou, M. (2024). *Strong screening rules for group-based SLOPE models*, https://arxiv.org/abs/2405.15357

## See Also

fit\_gslope()

Other gSLOPE-methods: coef.sgs(), fit\_goscar(), fit\_goscar\_cv(), fit\_gslope(), plot.sgs(), predict.sgs(), print.sgs()

Other model-selection: as\_sgs(), fit\_goscar\_cv(), fit\_sgo\_cv(), fit\_sgs\_cv(), scaled\_sgs()

## Examples

```
# specify a grouping structure
groups = c(1,1,1,2,2,3,3,3,4,4)
# generate data
data = gen_toy_data(p=10, n=5, groups = groups, seed_id=3,group_sparsity=1)
# run gSLOPE with cross-validation
cv_model = fit_gslope_cv(X = data$X, y = data$y, groups=groups, type = "linear", path_length = 5,
nfolds=5, gFDR = 0.1, min_frac = 0.05, standardise="12",intercept=TRUE,verbose=TRUE)
```

fit\_sgo

#### Description

Sparse-group OSCAR (SGO) main fitting function. Supports both linear and logistic regression, both with dense and sparse matrix implementations.

#### Usage

```
fit_sgo(
 Χ,
 у,
 groups,
  type = "linear",
 lambda = "path",
 path_length = 20,
 min_frac = 0.05,
 alpha = 0.95,
 max_iter = 5000,
 backtracking = 0.7,
 max_iter_backtracking = 100,
  tol = 1e-05,
  standardise = "12",
  intercept = TRUE,
  screen = TRUE,
  verbose = FALSE,
 w_weights = NULL,
 v_weights = NULL,
 warm_start = NULL
)
```

Х	Input matrix of dimensions $n \times p$ . Can be a sparse matrix (using class "sparseMatrix" from the Matrix package).
У	Output vector of dimension $n$ . For type="linear" should be continuous and for type="logistic" should be a binary variable.
groups	A grouping structure for the input data. Should take the form of a vector of group indices.
type	The type of regression to perform. Supported values are: "linear" and "logistic".
lambda	The regularisation parameter. Defines the level of sparsity in the model. A higher value leads to sparser models:
	<ul> <li>"path" computes a path of regularisation parameters of length "path_length". The path will begin just above the value at which the first predictor enters the model and will terminate at the value determined by "min_frac".</li> </ul>

	• User-specified single value or sequence. Internal scaling is applied based on the type of standardisation. The returned "lambda" value will be the original unscaled value(s).
path_length	The number of $\lambda$ values to fit the model for. If "lambda" is user-specified, this is ignored.
min_frac	Smallest value of $\lambda$ as a fraction of the maximum value. That is, the final $\lambda$ will be "min_frac" of the first $\lambda$ value.
alpha	The value of $\alpha$ , which defines the convex balance between OSCAR and gOSCAR. Must be between 0 and 1. Recommended value is 0.95.
max_iter	Maximum number of ATOS iterations to perform.
backtracking	The backtracking parameter, $\tau$ , as defined in Pedregosa and Gidel (2018).
<pre>max_iter_backt</pre>	racking Maximum number of backtracking line search iterations to perform per global iteration.
tol	Convergence tolerance for the stopping criteria.
standardise	Type of standardisation to perform on X:
	• "12" standardises the input data to have $\ell_2$ norms of one. When using this "lambda" is scaled internally by $1/\sqrt{n}$ .
	• "11" standardises the input data to have $\ell_1$ norms of one. When using this "lambda" is scaled internally by $1/n$ .
	• "sd" standardises the input data to have standard deviation of one.
	<ul> <li>"noBaone" no standardisation applied.</li> </ul>
intercept	Logical flag for whether to fit an intercept.
screen	Logical flag for whether to apply screening rules (see Feser and Evangelou (2024)). Screening discards irrelevant groups before fitting, greatly improving speed.
verbose	Logical flag for whether to print fitting information.
w_weights	Optional vector for the group penalty weights. Overrides the OSCAR penalties when specified. When entering custom weights, these are multiplied internally by $\lambda$ and $1 - \alpha$ . To void this behaviour, set $\lambda = 2$ and $\alpha = 0.5$ .
v_weights	Optional vector for the variable penalty weights. Overrides the OSCAR penal- ties when specified. When entering custom weights, these are multiplied inter- nally by $\lambda$ and $\alpha$ . To void this behaviour, set $\lambda = 2$ and $\alpha = 0.5$ .
warm_start	Optional list for implementing warm starts. These values are used as initial values in the fitting algorithm. Need to supply "x" and "u" in the form "list(warm_x, warm_u)". Not recommended for use with a path or CV fit as start from the null model by design.

## Details

fit\_sgo() fits an SGO model (Feser and Evangelou (2024)) using adaptive three operator splitting (ATOS). SGO uses the same model set-up as for SGS, but with different weights (see Bao et al.

## fit\_sgo

(2020) and Feser and Evangelou (2024)). The penalties are given by (for a group g and variable i, with p variables and m groups):

$$v_i = \sigma_1 + \sigma_2(p-i), \ w_g = \sigma_1 + \sigma_3(m-g),$$

where

$$\sigma_1 = d_i \| X^{\mathsf{T}} y \|_{\infty}, \ \sigma_2 = \sigma_1 / p, \ \sigma_3 = \sigma_1 / m, \ d_i = i \times \exp\left(-2\right).$$

## Value

A list containing:

beta	The fitted values from the regression. Taken to be the more stable fit between $x$ and $z$ , which is usually the former. A filter is applied to remove very small values, where ATOS has not been able to shrink exactly to zero. Check this against $x$ and $z$ .
group_effects	The group values from the regression. Taken by applying the $\ell_2$ norm within each group on beta.
selected_var	A list containing the indicies of the active/selected variables for each "lambda" value. Index 1 corresponds to the first column in X.
selected_grp	A list containing the indicies of the active/selected groups for each "lambda" value. Index 1 corresponds to the first group in the groups vector. You can see the group order by running unique(groups).
num_it	Number of iterations performed. If convergence is not reached, this will be max_iter.
success	Logical flag indicating whether ATOS converged, according to tol.
certificate	Final value of convergence criteria.
х	The solution to the original problem (see Pedregosa and Gidel (2018)).
Z	The updated values from applying the first proximal operator (see Pedregosa and Gidel (2018)).
u	The solution to the dual problem (see Pedregosa and Gidel (2018)).
<pre>screen_set_var</pre>	List of variables that were kept after screening step for each "lambda" value. (corresponds to $S_v$ in Feser and Evangelou (2024)).
<pre>screen_set_grp</pre>	List of groups that were kept after screening step for each "lambda" value. (corresponds to $S_g$ in Feser and Evangelou (2024)).
epsilon_set_var	
	List of variables that were used for fitting after screening for each "lambda" value. (corresponds to $\mathcal{E}_v$ in Feser and Evangelou (2024)).
epsilon_set_grp	
	List of groups that were used for fitting after screening for each "lambda" value. (corresponds to $\mathcal{E}_g$ in Feser and Evangelou (2024)).
kkt_violations_	
	List of variables that violated the KKT conditions each "lambda" value. (corresponds to $\mathcal{K}_v$ in Feser and Evangelou (2024)).

kkt_violations_grp		
	List of groups that violated the KKT conditions each "lambda" value. (corresponds to $\mathcal{K}_g$ in Feser and Evangelou (2024)).	
pen_slope	Vector of the variable penalty sequence.	
pen_gslope	Vector of the group penalty sequence.	
screen	Logical flag indicating whether screening was performed.	
type	Indicates which type of regression was performed.	
intercept	Logical flag indicating whether an intercept was fit.	
lambda	Value(s) of $\lambda$ used to fit the model.	

#### References

Bao, R., Gu B., Huang, H. (2020). *Fast OSCAR and OWL Regression via Safe Screening Rules*, https://proceedings.mlr.press/v119/bao20b

Feser, F., Evangelou, M. (2023). Sparse-group SLOPE: adaptive bi-level selection with FDRcontrol, https://arxiv.org/abs/2305.09467

Feser, F., Evangelou, M. (2024). *Strong screening rules for group-based SLOPE models*, https://arxiv.org/abs/2405.15357

Pedregosa, F., Gidel, G. (2018). *Adaptive Three Operator Splitting*, https://proceedings.mlr.press/v80/pedregosa18a.html

## See Also

Other SGS-methods: as\_sgs(), coef.sgs(), fit\_sgo\_cv(), fit\_sgs(), fit\_sgs\_cv(), plot.sgs(), predict.sgs(), print.sgs(), scaled\_sgs()

### Examples

```
# specify a grouping structure
groups = c(1,1,1,2,2,3,3,3,4,4)
# generate data
data = gen_toy_data(p=10, n=5, groups = groups, seed_id=3,group_sparsity=1)
# run SG0
model = fit_sgo(X = data$X, y = data$y, groups = groups, type="linear", path_length = 5,
alpha=0.95, standardise = "l2", intercept = TRUE, verbose=FALSE)
```

fit\_sgo\_cv

```
Fit an SGO model using k-fold cross-validation.
```

#### Description

Function to fit a pathwise solution of sparse-group SLOPE (SGO) models using k-fold cross-validation. Supports both linear and logistic regression, both with dense and sparse matrix implementations.

fit\_sgo\_cv

## Usage

```
fit_sgo_cv(
 Χ,
 у,
  groups,
  type = "linear",
 lambda = "path",
 path_length = 20,
 min_frac = 0.05,
 alpha = 0.95,
  nfolds = 10,
  backtracking = 0.7,
 max_{iter} = 5000,
 max_iter_backtracking = 100,
  tol = 1e-05,
  standardise = "12",
  intercept = TRUE,
  error_criteria = "mse",
  screen = TRUE,
 verbose = FALSE,
 v_weights = NULL,
 w_weights = NULL,
 warm_start = NULL
)
```

Х	Input matrix of dimensions $n \times p$ . Can be a sparse matrix (using class "sparseMatrix" from the Matrix package).
У	Output vector of dimension $n$ . For type="linear" should be continuous and for type="logistic" should be a binary variable.
groups	A grouping structure for the input data. Should take the form of a vector of group indices.
type	The type of regression to perform. Supported values are: "linear" and "logistic".
lambda	The regularisation parameter. Defines the level of sparsity in the model. A higher value leads to sparser models:
	• "path" computes a path of regularisation parameters of length "path_length". The path will begin just above the value at which the first predictor enters the model and will terminate at the value determined by "min_frac".
	• User-specified single value or sequence. Internal scaling is applied based on the type of standardisation. The returned "lambda" value will be the original unscaled value(s).
path_length	The number of $\lambda$ values to fit the model for. If "lambda" is user-specified, this is ignored.
min_frac	Smallest value of $\lambda$ as a fraction of the maximum value. That is, the final $\lambda$ will be "min_frac" of the first $\lambda$ value.

alpha	The value of $\alpha$ , which defines the convex balance between OSCAR and gOSCAR. Must be between 0 and 1. Recommended value is 0.95.
nfolds	The number of folds to use in cross-validation.
backtracking	The backtracking parameter, $\tau$ , as defined in Pedregosa and Gidel (2018).
<pre>max_iter</pre>	Maximum number of ATOS iterations to perform.
<pre>max_iter_backtr</pre>	-
	Maximum number of backtracking line search iterations to perform per global iteration.
tol	Convergence tolerance for the stopping criteria.
standardise	Type of standardisation to perform on X:
	• "12" standardises the input data to have $\ell_2$ norms of one.
	• "11" standardises the input data to have $\ell_1$ norms of one.
	• "sd" standardises the input data to have standard deviation of one.
	<ul> <li>"none" no standardisation applied.</li> </ul>
intercept	Logical flag for whether to fit an intercept.
error_criteria	The criteria used to discriminate between models along the path. Supported values are: "mse" (mean squared error) and "mae" (mean absolute error).
screen	Logical flag for whether to apply screening rules (see Feser and Evangelou (2024)). Screening discards irrelevant groups before fitting, greatly improving speed.
verbose	Logical flag for whether to print fitting information.
v_weights	Optional vector for the variable penalty weights. Overrides the OSCAR penal- ties when specified. When entering custom weights, these are multiplied inter- nally by $\lambda$ and $\alpha$ . To void this behaviour, set $\lambda = 2$ and $\alpha = 0.5$ .
w_weights	Optional vector for the group penalty weights. Overrides the OSCAR penalties when specified. When entering custom weights, these are multiplied internally by $\lambda$ and $1 - \alpha$ . To void this behaviour, set $\lambda = 2$ and $\alpha = 0.5$ .
warm_start	Optional list for implementing warm starts. These values are used as initial values in the fitting algorithm. Need to supply "x" and "u" in the form "list(warm_x, warm_u)". Not recommended for use with a path or CV fit as start from the null model by design.

## Details

Fits SGO models under a pathwise solution using adaptive three operator splitting (ATOS), picking the 1se model as optimum. Warm starts are implemented.

## Value

A list containing:

all_models	A list of all the models fitted along the path.
fit	The 1se chosen model, which is a "sgs" object type.
best_lambda	The value of $\lambda$ which generated the chosen model.

#### fit\_sgs

<pre>best_lambda_id</pre>	The path index for the chosen model.
errors	A table containing fitting information about the models on the path.
type	Indicates which type of regression was performed.

## References

Bao, R., Gu B., Huang, H. (2020). *Fast OSCAR and OWL Regression via Safe Screening Rules*, https://proceedings.mlr.press/v119/bao20b

Feser, F., Evangelou, M. (2023). Sparse-group SLOPE: adaptive bi-level selection with FDRcontrol, https://arxiv.org/abs/2305.09467

Feser, F., Evangelou, M. (2024). *Strong screening rules for group-based SLOPE models*, https://arxiv.org/abs/2405.15357

#### See Also

## fit\_sgo()

Other model-selection: as\_sgs(), fit\_goscar\_cv(), fit\_gslope\_cv(), fit\_sgs\_cv(), scaled\_sgs()
Other SGS-methods: as\_sgs(), coef.sgs(), fit\_sgo(), fit\_sgs(), fit\_sgs\_cv(), plot.sgs(),
predict.sgs(), print.sgs(), scaled\_sgs()

#### Examples

```
# specify a grouping structure
groups = c(1,1,1,2,2,3,3,3,4,4)
# generate data
data = gen_toy_data(p=10, n=5, groups = groups, seed_id=3,group_sparsity=1)
# run SGO with cross-validation
cv_model = fit_sgo_cv(X = data$X, y = data$y, groups=groups, type = "linear",
path_length = 5, nfolds=5, alpha = 0.95, min_frac = 0.05,
standardise="l2",intercept=TRUE,verbose=TRUE)
```

fit\_sgs

Fit an SGS model.

#### Description

Sparse-group SLOPE (SGS) main fitting function. Supports both linear and logistic regression, both with dense and sparse matrix implementations.

## Usage

```
fit_sgs(
   X,
   y,
   groups,
   type = "linear",
```

```
lambda = "path",
path_length = 20,
min_frac = 0.05,
alpha = 0.95,
vFDR = 0.1,
gFDR = 0.1,
pen_method = 1,
max_iter = 5000,
backtracking = 0.7,
max_iter_backtracking = 100,
tol = 1e-05,
standardise = "12",
intercept = TRUE,
screen = TRUE,
verbose = FALSE,
w_weights = NULL,
v_weights = NULL,
warm_start = NULL
```

```
)
```

Х	Input matrix of dimensions $n \times p$ . Can be a sparse matrix (using class "sparseMatrix" from the Matrix package).
У	Output vector of dimension $n$ . For type="linear" should be continuous and for type="logistic" should be a binary variable.
groups	A grouping structure for the input data. Should take the form of a vector of group indices.
type	The type of regression to perform. Supported values are: "linear" and "logistic".
lambda	The regularisation parameter. Defines the level of sparsity in the model. A higher value leads to sparser models:
	<ul> <li>"path" computes a path of regularisation parameters of length "path_length". The path will begin just above the value at which the first predictor enters the model and will terminate at the value determined by "min_frac".</li> <li>User-specified single value or sequence. Internal scaling is applied based on the type of standardisation. The returned "lambda" value will be the original unscaled value(s).</li> </ul>
path_length	The number of $\lambda$ values to fit the model for. If "lambda" is user-specified, this is ignored.
min_frac	Smallest value of $\lambda$ as a fraction of the maximum value. That is, the final $\lambda$ will be "min_frac" of the first $\lambda$ value.
alpha	The value of $\alpha$ , which defines the convex balance between SLOPE and gSLOPE. Must be between 0 and 1. Recommended value is 0.95.
vFDR	Defines the desired variable false discovery rate (FDR) level, which determines the shape of the variable penalties. Must be between 0 and 1.

fit\_sgs

gFDR	Defines the desired group false discovery rate (FDR) level, which determines the shape of the group penalties. Must be between 0 and 1.
pen_method	<ul> <li>The type of penalty sequences to use (see Feser and Evangelou (2023)):</li> <li>"1" uses the vMean SGS and gMean gSLOPE sequences.</li> <li>"2" uses the vMax SGS and gMean gSLOPE sequences.</li> <li>"3" uses the BH SLOPE and gMean gSLOPE sequences, also known as SGS Original.</li> </ul>
<pre>max_iter</pre>	Maximum number of ATOS iterations to perform.
backtracking max_iter_backt	The backtracking parameter, $ au$ , as defined in Pedregosa and Gidel (2018). racking
	Maximum number of backtracking line search iterations to perform per global iteration.
tol	Convergence tolerance for the stopping criteria.
standardise	Type of standardisation to perform on X:
	• "12" standardises the input data to have $\ell_2$ norms of one. When using this "lambda" is scaled internally by $1/\sqrt{n}$ .
	<ul> <li>"11" standardises the input data to have ℓ₁ norms of one. When using this "lambda" is scaled internally by 1/n.</li> <li>"sd" standardises the input data to have standard deviation of one.</li> </ul>
	<ul> <li>"none" no standardisation applied.</li> </ul>
intercept	Logical flag for whether to fit an intercept.
screen	Logical flag for whether to apply screening rules (see Feser and Evangelou (2024)). Screening discards irrelevant groups before fitting, greatly improving speed.
verbose	Logical flag for whether to print fitting information.
w_weights	Optional vector for the group penalty weights. Overrides the penalties from pen_method if specified. When entering custom weights, these are multiplied internally by $\lambda$ and $1 - \alpha$ . To void this behaviour, set $\lambda = 2$ and $\alpha = 0.5$ .
v_weights	Optional vector for the variable penalty weights. Overrides the penalties from pen_method if specified. When entering custom weights, these are multiplied internally by $\lambda$ and $\alpha$ . To void this behaviour, set $\lambda = 2$ and $\alpha = 0.5$ .
warm_start	Optional list for implementing warm starts. These values are used as initial values in the fitting algorithm. Need to supply "x" and "u" in the form "list(warm_x, warm_u)". Not recommended for use with a path or CV fit as start from the null model by design.

#### Details

fit\_sgs() fits an SGS model (Feser and Evangelou (2023)) using adaptive three operator splitting (ATOS). SGS is a sparse-group method, so that it selects both variables and groups. Unlike group selection approaches, not every variable within a group is set as active. It solves the convex optimisation problem given by

$$\frac{1}{2n}f(b;y,\mathbf{X}) + \lambda\alpha \sum_{i=1}^{p} v_i |b|_{(i)} + \lambda(1-\alpha) \sum_{g=1}^{m} w_g \sqrt{p_g} ||b^{(g)}||_2,$$

where  $f(\cdot)$  is the loss function and  $p_g$  are the group sizes. The penalty parameters in SGS are sorted so that the largest coefficients are matched with the largest penalties, to reduce the FDR. For the variables:  $|\beta|_{(1)} \ge \ldots \ge |\beta|_{(p)}$  and  $v_1 \ge \ldots \ge v_p \ge 0$ . For the groups:  $\sqrt{p_1} ||\beta^{(1)}||_2 \ge \ldots \ge \sqrt{p_m} ||\beta^{(m)}||_2$  and  $w_1 \ge \ldots \ge w_g \ge 0$ . In the case of the linear model, the loss function is given by the mean-squared error loss:

$$f(b; y, \mathbf{X}) = \|y - \mathbf{X}b\|_2^2$$

In the logistic model, the loss function is given by

$$f(b; y, \mathbf{X}) = -1/n \log(\mathcal{L}(b; y, \mathbf{X})).$$

where the log-likelihood is given by

$$\mathcal{L}(b; y, \mathbf{X}) = \sum_{i=1}^{n} \left\{ y_i b^{\mathsf{T}} x_i - \log(1 + \exp(b^{\mathsf{T}} x_i)) \right\}.$$

SGS can be seen to be a convex combination of SLOPE and gSLOPE, balanced through alpha, such that it reduces to SLOPE for alpha = 1 and to gSLOPE for alpha = 0. The penalty parameters in SGS are sorted so that the largest coefficients are matched with the largest penalties, to reduce the FDR. For the group penalties, see fit\_gslope(). For the variable penalties, the vMean SGS sequence (pen\_method=1) (Feser and Evangelou (2023)) is given by

$$v_i^{\text{mean}} = \overline{F}_{\mathcal{N}}^{-1} \left( 1 - \frac{q_v i}{2p} \right), \text{ where } \overline{F}_{\mathcal{N}}(x) := \frac{1}{m} \sum_{j=1}^m F_{\mathcal{N}} \left( \alpha x + \frac{1}{3} (1 - \alpha) a_j w_j \right), \ i = 1, \dots, p,$$

where  $F_N$  is the cumulative distribution functions of a standard Gaussian distribution. The vMax SGS sequence (pen\_method=2) (Feser and Evangelou (2023)) is given by

$$v_i^{\max} = \max_{j=1,\dots,m} \left\{ \frac{1}{\alpha} F_{\mathcal{N}}^{-1} \left( 1 - \frac{q_v i}{2p} \right) - \frac{1}{3\alpha} (1 - \alpha) a_j w_j \right\},\,$$

The BH SLOPE sequence (pen\_method=3) (Bogdan et al. (2015)) is given by

$$v_i = z(1 - iq_v/2p),$$

where z is the quantile function of a standard normal distribution.

## Value

A list containing:

beta	The fitted values from the regression. Taken to be the more stable fit between x and z, which is usually the former. A filter is applied to remove very small values, where ATOS has not been able to shrink exactly to zero. Check this against x and z.
group_effects	The group values from the regression. Taken by applying the $\ell_2$ norm within each group on beta.
selected_var	A list containing the indicies of the active/selected variables for each "lambda"

value. Index 1 corresponds to the first column in X.

selected_grp	A list containing the indicies of the active/selected groups for each "lambda" value. Index 1 corresponds to the first group in the groups vector. You can see the group order by running unique(groups).
num_it	Number of iterations performed. If convergence is not reached, this will be ${\tt max\_iter}.$
success	Logical flag indicating whether ATOS converged, according to tol.
certificate	Final value of convergence criteria.
x	The solution to the original problem (see Pedregosa and Gidel (2018)).
Z	The updated values from applying the first proximal operator (see Pedregosa and Gidel (2018)).
u	The solution to the dual problem (see Pedregosa and Gidel (2018)).
screen_set_var	List of variables that were kept after screening step for each "lambda" value. (corresponds to $S_v$ in Feser and Evangelou (2024)).
<pre>screen_set_grp</pre>	List of groups that were kept after screening step for each "lambda" value. (corresponds to $S_g$ in Feser and Evangelou (2024)).
epsilon_set_var	
	List of variables that were used for fitting after screening for each "lambda" value. (corresponds to $\mathcal{E}_v$ in Feser and Evangelou (2024)).
epsilon_set_grp	
	List of groups that were used for fitting after screening for each "lambda" value. (corresponds to $\mathcal{E}_g$ in Feser and Evangelou (2024)).
kkt_violations_	
	List of variables that violated the KKT conditions each "lambda" value. (corresponds to $\mathcal{K}_v$ in Feser and Evangelou (2024)).
kkt_violations_	
	List of groups that violated the KKT conditions each "lambda" value. (corresponds to $\mathcal{K}_g$ in Feser and Evangelou (2024)).
pen_slope	Vector of the variable penalty sequence.
pen_gslope	Vector of the group penalty sequence.
screen	Logical flag indicating whether screening was performed.
type	Indicates which type of regression was performed.
intercept	Logical flag indicating whether an intercept was fit.
lambda	Value(s) of $\lambda$ used to fit the model.

## References

Bogdan, M., van den Berg, E., Sabatti, C., Candes, E. (2015). *SLOPE - Adaptive variable selection via convex optimization*, https://projecteuclid.org/journals/annals-of-applied-statistics/volume-9/issue-3/SLOPEAdaptive-variable-selection-via-convex-optimization/10.1214/15-A0AS842.full

Feser, F., Evangelou, M. (2023). *Sparse-group SLOPE: adaptive bi-level selection with FDR-control*, https://arxiv.org/abs/2305.09467

Feser, F., Evangelou, M. (2024). *Strong screening rules for group-based SLOPE models*, https://arxiv.org/abs/2405.15357

Pedregosa, F., Gidel, G. (2018). *Adaptive Three Operator Splitting*, https://proceedings.mlr.press/v80/pedregosa18a.html

## See Also

Other SGS-methods: as\_sgs(), coef.sgs(), fit\_sgo(), fit\_sgo\_cv(), fit\_sgs\_cv(), plot.sgs(), predict.sgs(), print.sgs(), scaled\_sgs()

## Examples

```
# specify a grouping structure
groups = c(1,1,1,2,2,3,3,3,4,4)
# generate data
data = gen_toy_data(p=10, n=5, groups = groups, seed_id=3,group_sparsity=1)
# run SGS
model = fit_sgs(X = data$X, y = data$y, groups = groups, type="linear", path_length = 5,
alpha=0.95, vFDR=0.1, gFDR=0.1, standardise = "l2", intercept = TRUE, verbose=FALSE)
```

fit\_sgs\_cv

Fit an SGS model using k-fold cross-validation.

#### Description

Function to fit a pathwise solution of sparse-group SLOPE (SGS) models using k-fold cross-validation. Supports both linear and logistic regression, both with dense and sparse matrix implementations.

#### Usage

```
fit_sgs_cv(
 Х,
 у,
  groups,
  type = "linear",
  lambda = "path",
  path_length = 20,
 min_frac = 0.05,
  alpha = 0.95,
  vFDR = 0.1,
  gFDR = 0.1,
  pen_method = 1,
 nfolds = 10,
 backtracking = 0.7,
 max_iter = 5000,
 max_iter_backtracking = 100,
  tol = 1e-05,
```

## fit\_sgs\_cv

```
standardise = "12",
intercept = TRUE,
error_criteria = "mse",
screen = TRUE,
verbose = FALSE,
v_weights = NULL,
w_weights = NULL,
warm_start = NULL
)
```

Х	Input matrix of dimensions $n \times p$ . Can be a sparse matrix (using class "sparseMatrix" from the Matrix package).
У	Output vector of dimension $n$ . For type="linear" should be continuous and for type="logistic" should be a binary variable.
groups	A grouping structure for the input data. Should take the form of a vector of group indices.
type	The type of regression to perform. Supported values are: "linear" and "logistic".
lambda	The regularisation parameter. Defines the level of sparsity in the model. A higher value leads to sparser models:
	<ul> <li>"path" computes a path of regularisation parameters of length "path_length". The path will begin just above the value at which the first predictor enters the model and will terminate at the value determined by "min_frac".</li> <li>User-specified single value or sequence. Internal scaling is applied based on the type of standardisation. The returned "lambda" value will be the original unscaled value(s).</li> </ul>
path_length	The number of $\lambda$ values to fit the model for. If "lambda" is user-specified, this is ignored.
min_frac	Smallest value of $\lambda$ as a fraction of the maximum value. That is, the final $\lambda$ will be "min_frac" of the first $\lambda$ value.
alpha	The value of $\alpha$ , which defines the convex balance between SLOPE and gSLOPE. Must be between 0 and 1. Recommended value is 0.95.
vFDR	Defines the desired variable false discovery rate (FDR) level, which determines the shape of the variable penalties. Must be between 0 and 1.
gFDR	Defines the desired group false discovery rate (FDR) level, which determines the shape of the group penalties. Must be between 0 and 1.
pen_method	The type of penalty sequences to use (see Feser and Evangelou (2023)):
	<ul> <li>"1" uses the vMean SGS and gMean gSLOPE sequences.</li> <li>"2" uses the vMax SGS and gMean gSLOPE sequences.</li> <li>"3" uses the BH SLOPE and gMean gSLOPE sequences, also known as SGS Original.</li> </ul>
nfolds	The number of folds to use in cross-validation.
backtracking	The backtracking parameter, $\tau$ , as defined in Pedregosa and Gidel (2018).

max_iter	Maximum number of ATOS iterations to perform.
<pre>max_iter_backtr</pre>	racking
	Maximum number of backtracking line search iterations to perform per global iteration.
tol	Convergence tolerance for the stopping criteria.
standardise	Type of standardisation to perform on X:
	<ul> <li>"12" standardises the input data to have l<sub>2</sub> norms of one.</li> <li>"11" standardises the input data to have l<sub>1</sub> norms of one.</li> <li>"sd" standardises the input data to have standard deviation of one.</li> <li>"none" no standardisation applied.</li> </ul>
intercept	Logical flag for whether to fit an intercept.
error_criteria	The criteria used to discriminate between models along the path. Supported values are: "mse" (mean squared error) and "mae" (mean absolute error).
screen	Logical flag for whether to apply screening rules (see Feser and Evangelou (2024)). Screening discards irrelevant groups before fitting, greatly improving speed.
verbose	Logical flag for whether to print fitting information.
v_weights	Optional vector for the variable penalty weights. Overrides the penalties from pen_method if specified. When entering custom weights, these are multiplied internally by $\lambda$ and $\alpha$ . To void this behaviour, set $\lambda = 2$ and $\alpha = 0.5$
w_weights	Optional vector for the group penalty weights. Overrides the penalties from pen_method if specified. When entering custom weights, these are multiplied internally by $\lambda$ and $1 - \alpha$ . To void this behaviour, set $\lambda = 2$ and $\alpha = 0.5$
warm_start	Optional list for implementing warm starts. These values are used as initial values in the fitting algorithm. Need to supply "x" and "u" in the form "list(warm_x, warm_u)". Not recommended for use with a path or CV fit as start from the null model by design.

## Details

Fits SGS models under a pathwise solution using adaptive three operator splitting (ATOS), picking the 1se model as optimum. Warm starts are implemented.

## Value

A list containing:

all_models	A list of all the models fitted along the path.
fit	The 1se chosen model, which is a "sgs" object type.
best_lambda	The value of $\lambda$ which generated the chosen model.
<pre>best_lambda_id</pre>	The path index for the chosen model.
errors	A table containing fitting information about the models on the path.
type	Indicates which type of regression was performed.

#### gen\_pens

#### References

Feser, F., Evangelou, M. (2023). Sparse-group SLOPE: adaptive bi-level selection with FDRcontrol, https://arxiv.org/abs/2305.09467

Feser, F., Evangelou, M. (2024). *Strong screening rules for group-based SLOPE models*, https://arxiv.org/abs/2405.15357

### See Also

fit\_sgs()

Other model-selection: as\_sgs(), fit\_goscar\_cv(), fit\_gslope\_cv(), fit\_sgo\_cv(), scaled\_sgs()
Other SGS-methods: as\_sgs(), coef.sgs(), fit\_sgo(), fit\_sgo\_cv(), fit\_sgs(), plot.sgs(),
predict.sgs(), print.sgs(), scaled\_sgs()

#### Examples

```
# specify a grouping structure
groups = c(1,1,1,2,2,3,3,3,4,4)
# generate data
data = gen_toy_data(p=10, n=5, groups = groups, seed_id=3,group_sparsity=1)
# run SGS with cross-validation
cv_model = fit_sgs_cv(X = data$X, y = data$y, groups=groups, type = "linear",
path_length = 5, nfolds=5, alpha = 0.95, vFDR = 0.1, gFDR = 0.1, min_frac = 0.05,
standardise="l2",intercept=TRUE,verbose=TRUE)
```

gen\_pens

Generate penalty sequences for SGS.

#### Description

Generates variable and group penalties for SGS.

#### Usage

gen\_pens(gFDR, vFDR, pen\_method, groups, alpha)

gFDR	Defines the desired group false discovery rate (FDR) level, which determines the shape of the group penalties.
vFDR	Defines the desired variable false discovery rate (FDR) level, which determines the shape of the variable penalties.
pen_method	The type of penalty sequences to use (see Feser and Evangelou (2023)):
	• "1" uses the vMean SGS and gMean gSLOPE sequences.
	<ul> <li>"2" uses the vMax SGS and gMean gSLOPE sequences.</li> </ul>
	• "3" uses the BH SLOPE and gMean gSLOPE sequences, also known as SGS Original.

gen\_pens

	• "4" uses the gMax gSLOPE sequence. For a gSLOPE model only.
groups	A grouping structure for the input data. Should take the form of a vector of group indices.
alpha	The value of $\alpha$ , defines the convex balance between SLOPE and gSLOPE.

## Details

The vMean and vMax SGS sequences are variable sequences derived specifically to give variable false discovery rate (FDR) control for SGS under orthogonal designs (see Feser and Evangelou (2023)). The BH SLOPE sequence is derived in Bodgan et al. (2015) and has links to the Benjamini-Hochberg critical values. The sequence provides variable FDR-control for SLOPE under orthogonal designs. The gMean gSLOPE sequence is derived in Brzyski et al. (2015) and provides group FDR-control for gSLOPE under orthogonal designs.

#### Value

A list containing:

pen\_slope\_org A vector of the variable penalty sequence. pen\_gslope\_org A vector of the group penalty sequence.

#### References

Bogdan, M., Van den Berg, E., Sabatti, C., Su, W., Candes, E. (2015). *SLOPE — Adaptive variable selection via convex optimization*, https://projecteuclid.org/journals/annals-of-applied-statistics/ volume-9/issue-3/SLOPEAdaptive-variable-selection-via-convex-optimization/10.1214/ 15-AOAS842.full

Brzyski, D., Gossmann, A., Su, W., Bodgan, M. (2019). *Group SLOPE – Adaptive Selection of Groups of Predictors*, https://www.tandfonline.com/doi/full/10.1080/01621459.2017. 1411269

Feser, F., Evangelou, M. (2023). Sparse-group SLOPE: adaptive bi-level selection with FDRcontrol, https://arxiv.org/abs/2305.09467

## Examples

gen\_toy\_data

## Description

Generates different types of datasets, which can then be fitted using sparse-group SLOPE.

## Usage

```
gen_toy_data(
 р,
  n,
  rho = 0,
  seed_id = 2,
  grouped = TRUE,
 groups,
 noise_level = 1,
  group_sparsity = 0.1,
 var_sparsity = 0.5,
 orthogonal = FALSE,
  data_mean = 0,
 data_sd = 1,
  signal_mean = 0,
  signal_sd = sqrt(10)
)
```

р	The number of input variables.
n	The number of observations.
rho	Correlation coefficient. Must be in range $[0, 1]$ .
seed_id	Seed to be used to generate the data matrix $X$ .
grouped	A logical flag indicating whether grouped data is required.
groups	If grouped=TRUE, the grouping structure is required. Each input variable should have a group id.
noise_level	Defines the level of noise $(\sigma)$ to be used in generating the response vector $y$ .
group_sparsity	Defines the level of group sparsity. Must be in the range $[0, 1]$ .
var_sparsity	Defines the level of variable sparsity. Must be in the range $[0,1]. \ \mbox{If grouped=TRUE}, this defines the level of sparsity within each group, not globally.}$
orthogonal	Logical flag as to whether the input matrix should be orthogonal.
data_mean	Defines the mean of input predictors.
data_sd	Defines the standard deviation of the signal $(\beta)$ .
signal_mean	Defines the mean of the signal $(\beta)$ .
signal_sd	Defines the standard deviation of the signal ( $\beta$ ).

## Details

The data is generated under a Gaussian linear model. The generated data can be grouped and sparsity can be provided at both a group and/or variable level.

## Value

A list containing:

У	The response vector.
Х	The input matrix.
true_beta	The true values of $\beta$ used to generate the response.
true_grp_id	Indices of which groups are non-zero in true_beta.

#### Examples

plot.sgs	Plot models of the following	object types:	"sgs", "sgs_cv",
	"gslope", "gslope_cv".		

## Description

Plots the pathwise solution of a cross-validation fit, from a call to one of the following: fit\_sgs(), fit\_sgs\_cv(), fit\_gslope(), fit\_gslope\_cv(), fit\_sgo(), fit\_sgo\_cv(), fit\_goscar(), fit\_goscar\_cv().

## Usage

## S3 method for class 'sgs'
plot(x, how\_many = 10, ...)

х	Object of one of the following classes: "sgs", "sgs_cv", "gslope", "gslope_cv".
how_many	Defines how many predictors to plot. Plots the predictors in decreasing order of largest absolute value.
	further arguments passed to base function.

#### predict.sgs

#### Value

A list containing:

response	The predicted response. In the logistic case, this represents the predicted class probabilities.
class	The predicted class assignments. Only returned if type = "logistic" in the model object.

## See Also

fit\_sgs(), fit\_sgs\_cv(), fit\_gslope(), fit\_gslope\_cv(), fit\_sgo(), fit\_sgo\_cv(), fit\_goscar(), fit\_goscar\_cv()

Other SGS-methods: as\_sgs(), coef.sgs(), fit\_sgo(), fit\_sgo\_cv(), fit\_sgs(), fit\_sgs\_cv(),
predict.sgs(), print.sgs(), scaled\_sgs()

Other gSLOPE-methods: coef.sgs(), fit\_goscar(), fit\_goscar\_cv(), fit\_gslope(), fit\_gslope\_cv(), predict.sgs(), print.sgs()

#### Examples

```
# specify a grouping structure
groups = c(1,1,2,2,3)
# generate data
data = gen_toy_data(p=5, n=4, groups = groups, seed_id=3,signal_mean=20,group_sparsity=1)
# run SGS
model = fit_sgs(X = data$X, y = data$y, groups=groups, type = "linear",
path_length = 20, alpha = 0.95, vFDR = 0.1, gFDR = 0.1,
min_frac = 0.05, standardise="l2",intercept=TRUE,verbose=FALSE)
plot(model, how_many = 10)
```

predict.sgs

Predict using one of the following object types: "sgs", "sgs\_cv", "gslope", "gslope\_cv".

#### Description

Performs prediction from one of the following fits: fit\_sgs(), fit\_sgs\_cv(), fit\_gslope(), fit\_gslope\_cv(), fit\_sgo(), fit\_sgo\_cv(), fit\_goscar(), fit\_goscar\_cv(). The predictions are calculated for each "lambda" value in the path.

#### Usage

```
## S3 method for class 'sgs'
predict(object, x, ...)
```

print.sgs

#### Arguments

object	Object of one of the following classes: "sgs", "sgs_cv", "gslope", "gslope_cv".
х	Input data to use for prediction.
	further arguments passed to stats function.

## Value

A list containing:

response	The predicted response. In the logistic case, this represents the predicted class probabilities.
class	The predicted class assignments. Only returned if type = "logistic" in the model object.

## See Also

fit\_sgs(), fit\_sgs\_cv(), fit\_gslope(), fit\_gslope\_cv(), fit\_sgo(), fit\_sgo\_cv(), fit\_goscar(), fit\_goscar\_cv()

Other SGS-methods: as\_sgs(), coef.sgs(), fit\_sgo(), fit\_sgo\_cv(), fit\_sgs(), fit\_sgs\_cv(),
plot.sgs(), print.sgs(), scaled\_sgs()

Other gSLOPE-methods: coef.sgs(), fit\_goscar(), fit\_goscar\_cv(), fit\_gslope(), fit\_gslope\_cv(),
plot.sgs(), print.sgs()

#### Examples

```
# specify a grouping structure
groups = c(1,1,1,2,2,3,3,3,4,4)
# generate data
data = gen_toy_data(p=10, n=5, groups = groups, seed_id=3,group_sparsity=1)
# run SGS
model = fit_sgs(X = data$X, y = data$y, groups = groups, type="linear", lambda = 1, alpha=0.95,
vFDR=0.1, gFDR=0.1, standardise = "l2", intercept = TRUE, verbose=FALSE)
# use predict function
model_predictions = predict(model, x = data$X)
```

print.sgs

Prints information for one of the following object types: "sgs", "sgs\_cv", "gslope", "gslope\_cv".

#### Description

Prints out useful metric from a model fit.

#### Usage

## S3 method for class 'sgs'
print(x, ...)

#### scaled\_sgs

#### Arguments

х	Object of one of the following classes: "sgs", "sgs_cv", "gslope", "gslope_cv".
•••	further arguments passed to base function.

## Value

A summary of the model fit(s).

#### See Also

fit\_sgs(), fit\_sgs\_cv(), fit\_gslope(), fit\_gslope\_cv(), fit\_sgo(), fit\_sgo\_cv(), fit\_goscar(), fit\_goscar\_cv()

```
Other SGS-methods: as_sgs(), coef.sgs(), fit_sgo(), fit_sgo_cv(), fit_sgs(), fit_sgs_cv(),
plot.sgs(), predict.sgs(), scaled_sgs()
```

OthergSLOPE-methods: coef.sgs(), fit\_goscar(), fit\_goscar\_cv(), fit\_gslope(), fit\_gslope\_cv(),
plot.sgs(), predict.sgs()

#### Examples

scaled\_sgs

Fits a scaled regression SLOPE-based.

#### Description

Fits a scaled regression SLOPE-based model using the noise estimation procedure (Algorithm 5 from Bogdan et al. (2015)). This estimates  $\lambda$  and then fits the model using the estimated value. It is an alternative approach to cross-validation (fit\_sgs\_cv()).

# Usage

```
scaled_sgs(
   X,
   y,
   groups,
   model = "sgs",
   type = "linear",
   pen_method = 1,
   alpha = 0.95,
   vFDR = 0.1,
   gFDR = 0.1,
   standardise = "l2",
   intercept = TRUE,
   verbose = FALSE
)
```

# Arguments

Х	Input matrix of dimensions $n \times p$ . Can be a sparse matrix (using class "sparseMatrix" from the Matrix package).	
У	Output vector of dimension $n$ . For type="linear" should be continuous and for type="logistic" should be a binary variable.	
groups	A grouping structure for the input data. Should take the form of a vector of group indices.	
model	The type of model to fit. Supported values are: "sgs" and "gslope".	
type	The type of regression to perform. Supported values are: "linear" and "logistic".	
pen_method	The type of penalty sequences to use.	
	• "1" uses the vMean SGS and gMean gSLOPE sequences. For the gSLOPE model, uses the mean sequence.	
	• "2" uses the vMax SGS and gMean gSLOPE sequences. For the gSLOPE model, uses the max sequence.	
	• "1" uses the BH SLOPE and gMean gSLOPE sequences, also known as SGS Original.	
alpha	The value of $\alpha$ , which defines the convex balance between SLOPE and gSLOPE. Must be between 0 and 1.	
vFDR	Defines the desired variable false discovery rate (FDR) level, which determines the shape of the variable penalties. Must be between 0 and 1.	
gFDR	Defines the desired group false discovery rate (FDR) level, which determines the shape of the group penalties. Must be between 0 and 1.	
standardise	Type of standardisation to perform on X:	
	• "12" standardises the input data to have $\ell_2$ norms of one.	
	• "11" standardises the input data to have $\ell_1$ norms of one.	
	• "sd" standardises the input data to have standard deviation of one.	
	• "none" no standardisation applied.	

42

#### scaled\_sgs

intercept	Logical flag for whether to fit an intercept.
verbose	Logical flag for whether to print fitting information.

#### Value

An object of type "sgs" containing model fit information (see fit\_sgs()).

## References

Bogdan, M., Van den Berg, E., Sabatti, C., Su, W., Candes, E. (2015). *SLOPE — Adaptive variable selection via convex optimization*, https://projecteuclid.org/journals/annals-of-applied-statistics/ volume-9/issue-3/SLOPEAdaptive-variable-selection-via-convex-optimization/10.1214/ 15-AOAS842.full

#### See Also

#### as\_sgs()

Other model-selection: as\_sgs(), fit\_goscar\_cv(), fit\_gslope\_cv(), fit\_sgo\_cv(), fit\_sgs\_cv()
Other SGS-methods: as\_sgs(), coef.sgs(), fit\_sgo(), fit\_sgo\_cv(), fit\_sgs(), fit\_sgs\_cv(),
plot.sgs(), predict.sgs(), print.sgs()

## Examples

```
# specify a grouping structure
groups = c(1,1,2,2,3)
# generate data
data = gen_toy_data(p=5, n=4, groups = groups, seed_id=3,
signal_mean=20,group_sparsity=1,var_sparsity=1)
# run noise estimation
model = scaled_sgs(X=data$X, y=data$y, groups=groups, pen_method=1)
```

# Index

\* SGS-methods as\_sgs. 3 coef.sgs, 7 fit\_sgo, 21 fit\_sgo\_cv, 24 fit\_sgs, 27 fit\_sgs\_cv, 32 plot.sgs, 38 predict.sgs, 39 print.sgs, 40 scaled\_sgs, 41 \* gSLOPE-methods coef.sgs, 7 fit\_goscar, 8 fit\_goscar\_cv, 11 fit\_gslope, 14 fit\_gslope\_cv, 18 plot.sgs, 38 predict.sgs, 39 print.sgs, 40 \* model-selection as\_sgs, 3 fit\_goscar\_cv, 11 fit\_gslope\_cv, 18 fit\_sgo\_cv, 24 fit\_sgs\_cv, 32 scaled\_sgs, 41 arma\_mv, 2 arma\_sparse, 3 as\_sgs, 3, 7, 13, 20, 24, 27, 32, 35, 39-41, 43 as\_sgs(), 43 atos. 5 coef.sgs, 4, 7, 11, 13, 17, 20, 24, 27, 32, 35, 39-41, 43 fit\_goscar, 7, 8, 13, 17, 20, 39-41 fit\_goscar(), 7, 13, 38-41

fit\_goscar\_cv, 4, 7, 11, 11, 17, 20, 27, 35, 39-41,43 fit\_goscar\_cv(), 7, 38-41 fit\_gslope, 7, 11, 13, 14, 20, 39-41 fit\_gslope(), 7, 20, 30, 38-41 fit\_gslope\_cv, 4, 7, 11, 13, 17, 18, 27, 35, 39-41, 43 fit\_gslope\_cv(), 7, 38-41 fit\_sgo, 4, 7, 21, 27, 32, 35, 39-41, 43 fit\_sgo(), 7, 27, 38-41 fit\_sgo\_cv, 4, 7, 13, 20, 24, 24, 32, 35, 39-41.43 fit\_sgo\_cv(), 7, 38-41 fit\_sgs, 4, 7, 24, 27, 27, 35, 39-41, 43 fit\_sgs(), 4, 7, 35, 38-41, 43 fit\_sgs\_cv, 4, 7, 13, 20, 24, 27, 32, 32, 39-41,43 fit\_sgs\_cv(), 3, 7, 38-41 gen\_pens, 35 gen\_toy\_data, 37 plot.sgs, 4, 7, 11, 13, 17, 20, 24, 27, 32, 35, 38, 40, 41, 43 predict.sgs, 4, 7, 11, 13, 17, 20, 24, 27, 32, 35, 39, 39, 41, 43 print.sgs, 4, 7, 11, 13, 17, 20, 24, 27, 32, 35, 39, 40, 40, 43 scaled\_sgs, 4, 7, 13, 20, 24, 27, 32, 35, *39–41*, 41

```
scaled_sgs(), 4
```