

# Mixture Analysis of the **Galaxy** Data Using the Package **mixAK**

Arnošt Komárek

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This document supplements a paper Komárek (2009) and shows an analysis of the Galaxy data introduced in the context of mixture modelling by Roeder (1990) using the R package **mixAK**.

## 1 Introduction

- Due to the fact that some code (especially MCMC) is time consuming, some code chunks found in this vignette are not run when compiling the package. You should set the variable **RUN.TIMECONSUMING.CODE** to **TRUE** to run full MCMC and related code.
- Having run full MCMC and related code, setting the variable **RUN.ALLOUT** to **TRUE** will cause that all output shown in this vignette is re-created and not taken from previously computed results.
- Results based on full MCMC runs are stored (chains excluded) in Galaxy-Result.RData in **./RESULT\_OBJ** directory and are used to create majority of this vignette at the time of compilation of the package.

**R⇒** Setting variables **RUN.ALLOUT** and **RUN.TIMECONSUMING.CODE**.

```
> RUN.TIMECONSUMING.CODE <- FALSE  
> RUN.ALLOUT <- FALSE
```

**R⇒** Directory to store postscript files with figures. Figures which require chains are stored in **FIGKEEPDIR** directory all other figures are stored in **FIGDIR** directory.

```
> FIGDIR <- "./figures/"  
> FIGKEEPDIR <- "./figuresKeep/"
```

**R⇒** Directories with results computed in past. Objects with chains will be stored in directory specified by variable **RESULTDIR**. All other objects will be stored in directory **RESULT2DIR**.

```
> RESULTDIR <- "/home/komarek/RESULT_OBJ/mixAK-Galaxy-S081115/"  
> RESULT2DIR <- "./RESULT_OBJ/"      ### available in package as /inst/doc/RESULT_OBJ
```

**R⇒** Display options.

```
> options(width = 80)
```

**R⇒** Load results computed in past.

```

> if (RUN.ALLOUT){
+   load(paste(RESULT2DIR, "Galaxy-Result.RData", sep=""))
+     ## contains RJModel2 (without chains), FixModel2 (without chains),
+     ##               PDensRJ2, PDensFix2
+   load(paste(RESULTDIR, "Galaxy-RJ2.RData", sep=""))
+     ## contains RJModel2 (contains chains as well)
+ }else{
+   load(paste(RESULT2DIR, "Galaxy-Result.RData", sep=""))
+     ## contains RJModel2 (without chains), FixModel2 (without chains),
+     ##               PDensRJ2, PDensFix2
+ }

```

**R⇒** Load the package `mixAK` and package `coda` which will be used to perform some basic convergence diagnostics.

```

> library("mixAK")
> library("coda")

```

## 2 Exploration of the data

R⇒ The data are read and summarized as follows.

```
> data("Galaxy", package = "mixAK")
> summary(Galaxy)
```

Min.	1st Qu.	Median	Mean	3rd Qu.	Max.
9.172	19.530	20.830	20.830	23.130	34.280

R⇒ Additionally, Figure 1 shows the histogram of the data.

```
> postscript(paste(FIGDIR, "figGalaxy01.ps", sep=""), width=6, height=6,
+           horizontal=FALSE)
> par(mfrow=c(1, 1), bty="n")
> hist(Galaxy, prob=TRUE, col="sandybrown", breaks=seq(7, 37, by=0.5),
+      xlab="Velocity (km/sec)", ylab="Density", main="")
> dev.off()
```

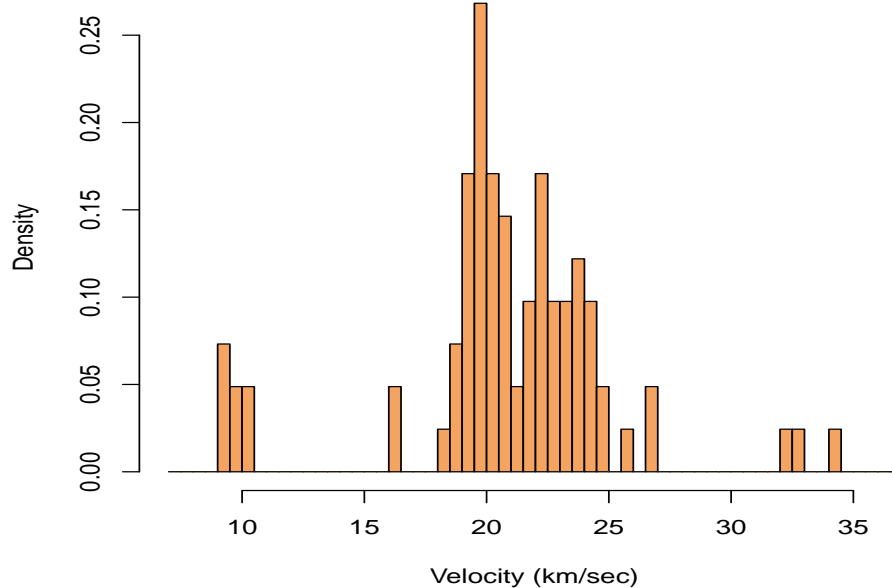


Figure 1: Histogram of Galaxy data.

### 3 Preparation of the MCMC

**R⇒** Length of the MCMC simulation for all models in this document (burn-in of 100 000 iterations, additional 500 000 iterations are kept for the inference, thinning 1:10):

```
> nMCMC <- c(burn=100000, keep=500000, thin=10, info=10000)
```

**R⇒** Grid of values where we evaluate and subsequently plot the predictive density for all models in this document:

```
> ygrid <- seq(5, 40, length = 500)
```

## 4 Model with a number of components estimated using the RJ-MCMC

### 4.1 Specification of the prior distributions and MCMC simulation

$\Rightarrow$  The minimal specification of the prior distribution and running RJ-MCMC with default values for all prior parameters:

```
> RJPrior1 <- list(priorK="uniform", Kmax=30)
> if (RUN.TIMECONSUMING.CODE){
+   RJModel1 <- NMixMCMC(y0=Galaxy, prior=RJPrior1, nMCMC=nMCMC,
+                       scale=list(shift=0, scale=1), PED=TRUE)
+ }
```

$\Rightarrow$  The prior distribution for the function `NMixMCMC` was the same as with

```
> RJPrior1 <- list(priorK="uniform", Kmax=30,
+                  delta=1,
+                  priormuQ="independentC", xi=21.7255, D=630.3614,
+                  zeta=2, g=0.2, h=0.01586391)
```

In the following, we will use the same prior hyperparameters and tuning parameters as in Richardson and Green (1997) when analyzing this dataset. Note that our prior for the mixture inverse variances is parametrized in terms of the Wishart distribution whereas Gamma distribution is used in Richardson and Green (1997). Hence our  $\zeta = 2 \cdot 2$  corresponds to  $\alpha = 2$  in [RG] and our  $h = 0.016/2$  corresponds to  $h = 0.016$  in [RG].

$\Rightarrow$  Prior distribution of Richardson and Green (1997):

```
> RJPrior2 <- list(priorK="uniform", Kmax=30,
+                  delta=1,
+                  priormuQ="independentC", xi=21.73, D=630.5121,
+                  zeta=2*2, g=0.2, h=0.016/2)
```

$\Rightarrow$  Parameters to tune RJ-MCMC:

```
> parRJMCMC2 <- list(par.u1=c(2, 2),
+                    par.u2=c(2, 2),
+                    par.u3=c(1, 1))
```

R⇒ Running the MCMC simulation.

R⇒ Two chains will be generated since the argument **PED** is set to **TRUE** (output is shown from MCMC simulation performed by author):

```
> if (RUN.TIMECONSUMING.CODE){  
+   set.seed(770328)  
+   RJModel2 <- NMixMCMC(y0=Galaxy, prior=RJPrior2, RJMCMC=parRJMCMC2,  
+                         nMCMC=nMCMC, scale=list(shift=0, scale=1), PED=TRUE)  
+ }
```

Chain number 1

=====

MCMC sampling started on Tue Nov 11 12:11:23 2008.

Burn-in iteration 100000

Iteration 600000

MCMC sampling finished on Tue Nov 11 12:22:08 2008.

Chain number 2

=====

MCMC sampling started on Tue Nov 11 12:22:09 2008.

Burn-in iteration 100000

Iteration 600000

MCMC sampling finished on Tue Nov 11 12:32:55 2008.

Computation of penalized expected deviance started on Tue Nov 11 12:32:57 2008.

Computation of penalized expected deviance finished on Tue Nov 11 12:36:54 2008.

R⇒ Information concerning the acceptance rates of different move types (separately for each chain):

```
> print(RJModel2[[1]]$moves)
```

	Performed	Accepted	Proportion accepted (%)
Gibbs with fixed K	5000000	5000000	100.00
Split	2502857	365907	14.62
Combine	2497143	384026	15.38
Birth	2501161	443183	17.72
Death	2498839	425063	17.01

```
> print(RJModel2[[2]]$moves)
```

	Performed	Accepted	Proportion accepted (%)
Gibbs with fixed K	5000000	5000000	100.00
Split	2500622	365327	14.61
Combine	2499378	381750	15.27
Birth	2502545	440529	17.60
Death	2497455	424109	16.98

## 4.2 Posterior inference

R⇒ Basic posterior summary of the fitted model:

```
> print(RJModel12)
```

```
Normal mixture with at most 30 components estimated using RJ-MCMC
=====
Posterior distribution of K:
-----
              1          2          3          4          5          6          7          8
Chain 1 0.000136 0.004636 0.035326 0.113576 0.21326 0.245938 0.185912 0.108304
Chain 2 0.000136 0.004774 0.036136 0.114488 0.21342 0.246008 0.185468 0.108172
              9          10          11          12          13          14          15          16
Chain 1 0.054128 0.023652 0.009674 0.003634 0.001196 0.000422 0.000140 5.8e-05
Chain 2 0.053236 0.023544 0.009230 0.003478 0.001356 0.000394 0.000108 3.4e-05
              17          18          19
Chain 1 4.0e-06 2e-06 2e-06
Chain 2 1.4e-05 4e-06 0e+00

Posterior summary statistics for moments of mixture for original data:
-----
Mean:
      Mean Std.Dev.      Min.      2.5% 1st Qu.  Median 3rd Qu.
Chain 1 20.85665 0.7665924  1.508469 19.65970 20.49000 20.86112 21.22509
Chain 2 20.85673 0.7699914 -6.239395 19.65688 20.49049 20.85974 21.22313
      97.5%      Max.
Chain 1 22.03940 57.56010
Chain 2 22.03613 49.30073

Standard deviation:
      Mean Std.Dev.      Min.      2.5% 1st Qu.  Median 3rd Qu.
Chain 1 5.024763 1.020024 0.06109612 3.810018 4.469011 4.852147 5.302620
Chain 2 5.023523 1.024113 0.02530225 3.809339 4.466287 4.850280 5.298962
      97.5%      Max.
Chain 1 7.681152 45.97838
Chain 2 7.682431 35.00435
```

R⇒ Computation of the predictive density (separately for chain 1 and chain 2):

```
> if (RUN.TIMECONSUMING.CODE) {  
+   PDensRJ2 <- list()  
+   PDensRJ2[[1]] <- NMixPredDensMarg(RJModel2[[1]], grid = ygrid)  
+   PDensRJ2[[2]] <- NMixPredDensMarg(RJModel2[[2]], grid = ygrid)  
+ }
```

R⇒ Default `plot` method for the computed object (see Figure 2):

```
> postscript(paste(FIGDIR, "figGalaxy02.ps", sep = ""), width = 6,  
+   height = 6, horizontal = FALSE)  
> par(mfrow = c(1, 1), bty = "n")  
> plot(PDensRJ2[[1]], xlab = "Velocity (km/sec)")  
> dev.off()
```

R⇒ Plots of conditional predictive densities (given  $K$ ) plus the overall predictive density (see Figure 3):

```
> postscript(paste(FIGDIR, "figGalaxy03.ps", sep=""), width=6, height=6,  
+   horizontal=FALSE)  
> par(mfrow=c(1, 1), bty="n")  
> plot(PDensRJ2[[1]], K=c(0, 4:7), xlab="Velocity (km/sec)",  
+   lty=c(1, rep(2, 4)), col=c("darkblue", rep("red", 4)),  
+   lwd=c(2, rep(1, 4)))  
> dev.off()
```

R⇒ Plot of the predictive density together with the histogram of the data for both chains (see Figure 4):

```
> postscript(paste(FIGDIR, "figGalaxy04.ps", sep=""), width=6, height=10,  
+   horizontal=FALSE)  
> par(mfrow=c(2, 1), bty="n")  
> #  
> ## Chain 1  
> hist(Galaxy, prob=TRUE, col="sandybrown",  
+   breaks=seq(7, 37, by=0.5),  
+   xlab="Velocity (km/sec)", ylab="Density", main="Chain 1")  
> lines(PDensRJ2[[1]]$x$x1, PDensRJ2[[1]]$dens[[1]],  
+   col="darkblue", lwd=2)  
> #  
> ## Chain 2  
> hist(Galaxy, prob=TRUE, col="sandybrown",  
+   breaks=seq(7, 37, by=0.5),  
+   xlab="Velocity (km/sec)", ylab="Density", main="Chain 2")  
> lines(PDensRJ2[[2]]$x$x1, PDensRJ2[[2]]$dens[[1]],  
+   col="darkblue", lwd=2)  
> dev.off()
```



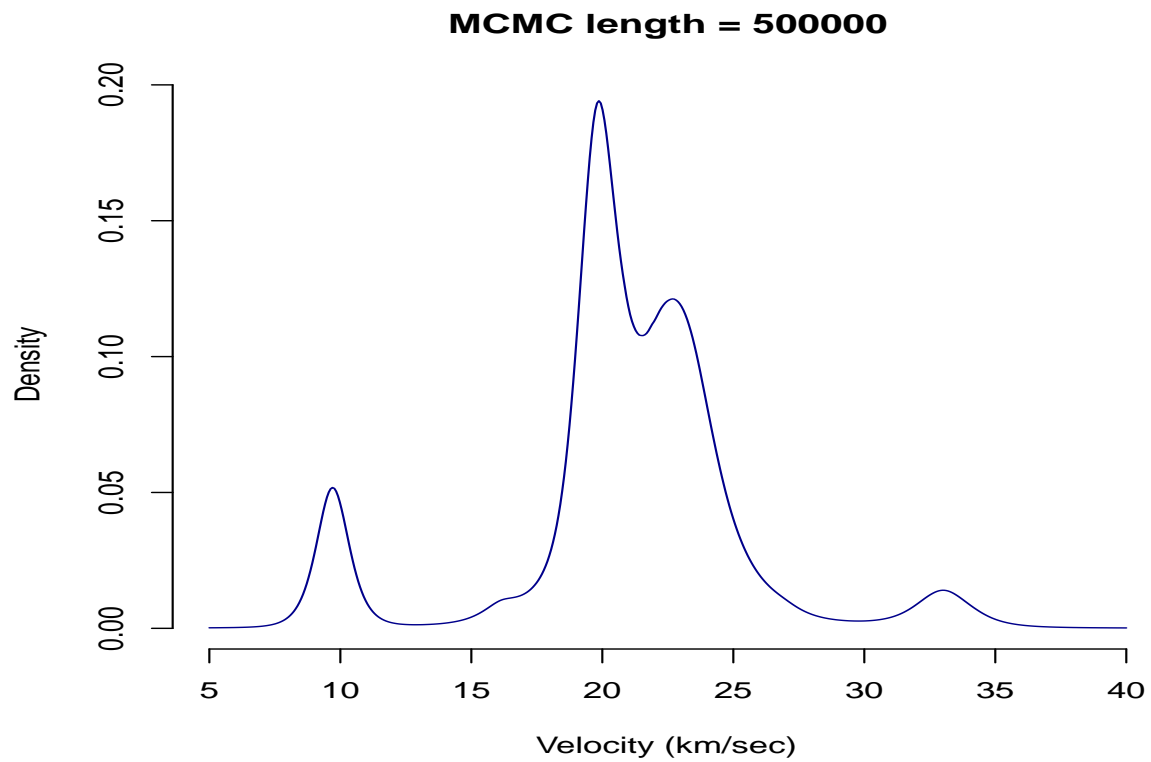


Figure 2: Predictive density based on the model with a random number of mixture components (results from chain 1).

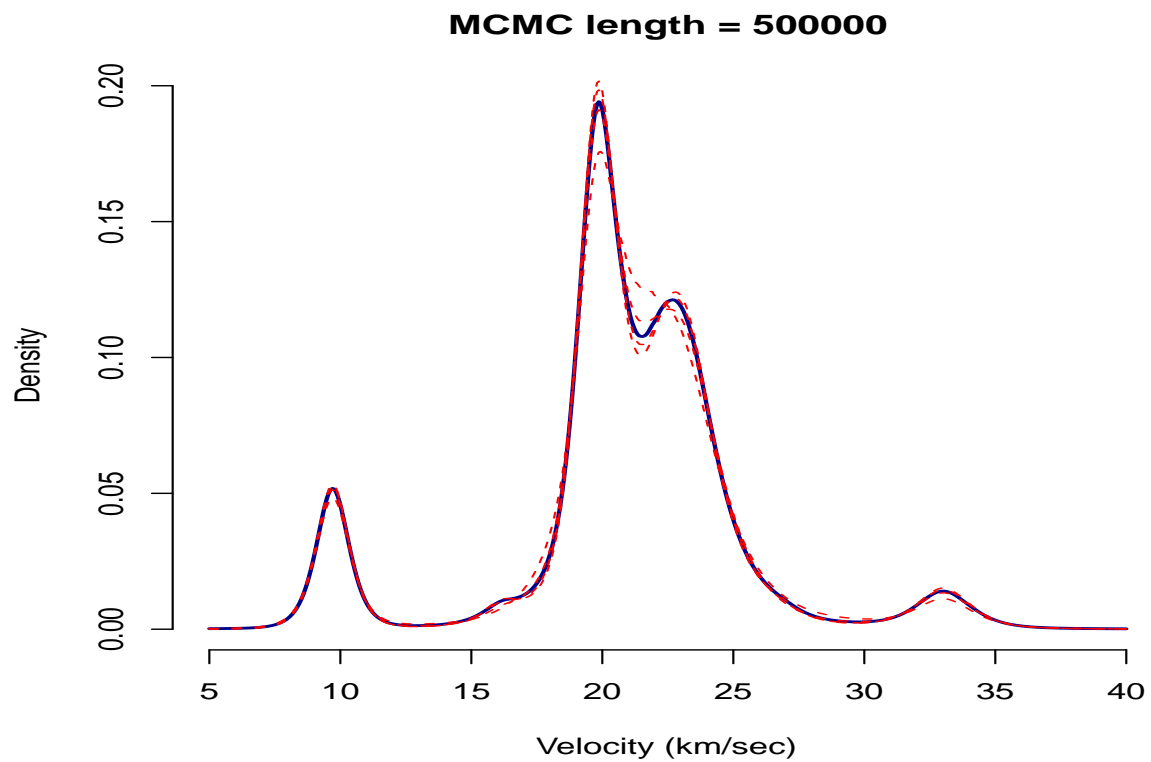


Figure 3: Overall predictive density based on the model with a random number of mixture components (in blue) and conditional predictive densities for  $K = 4, 5, 6, 7$  (in red), results from chain 1.

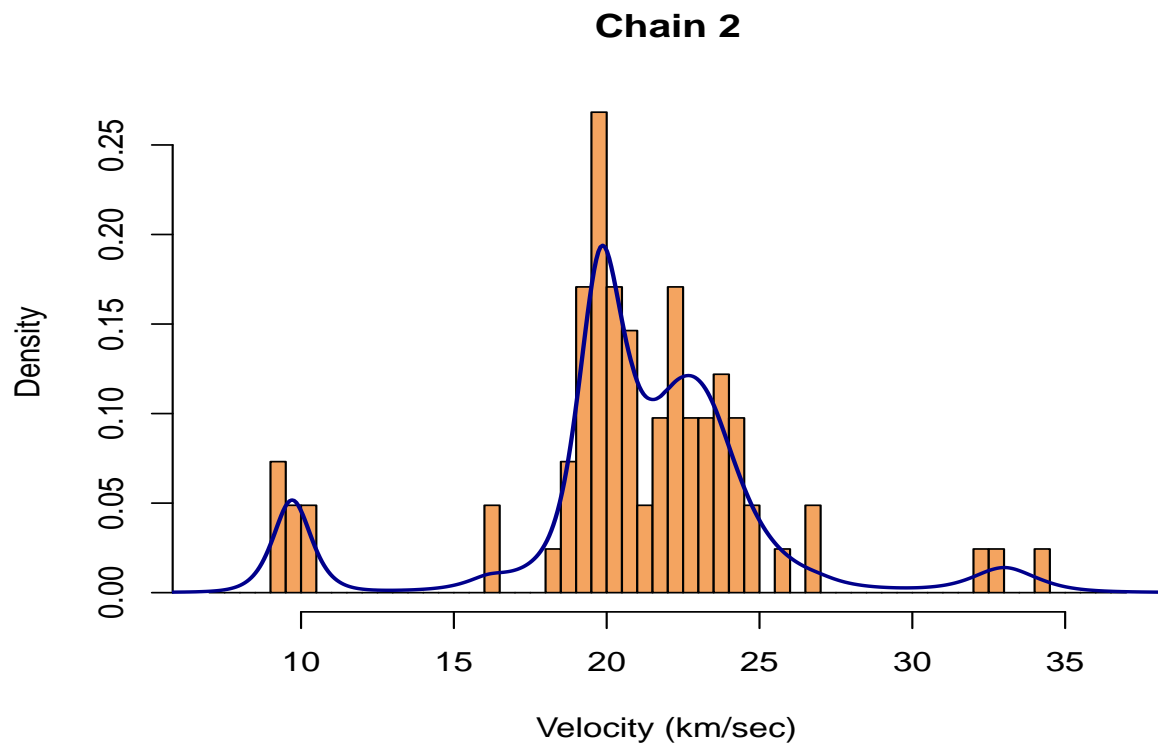
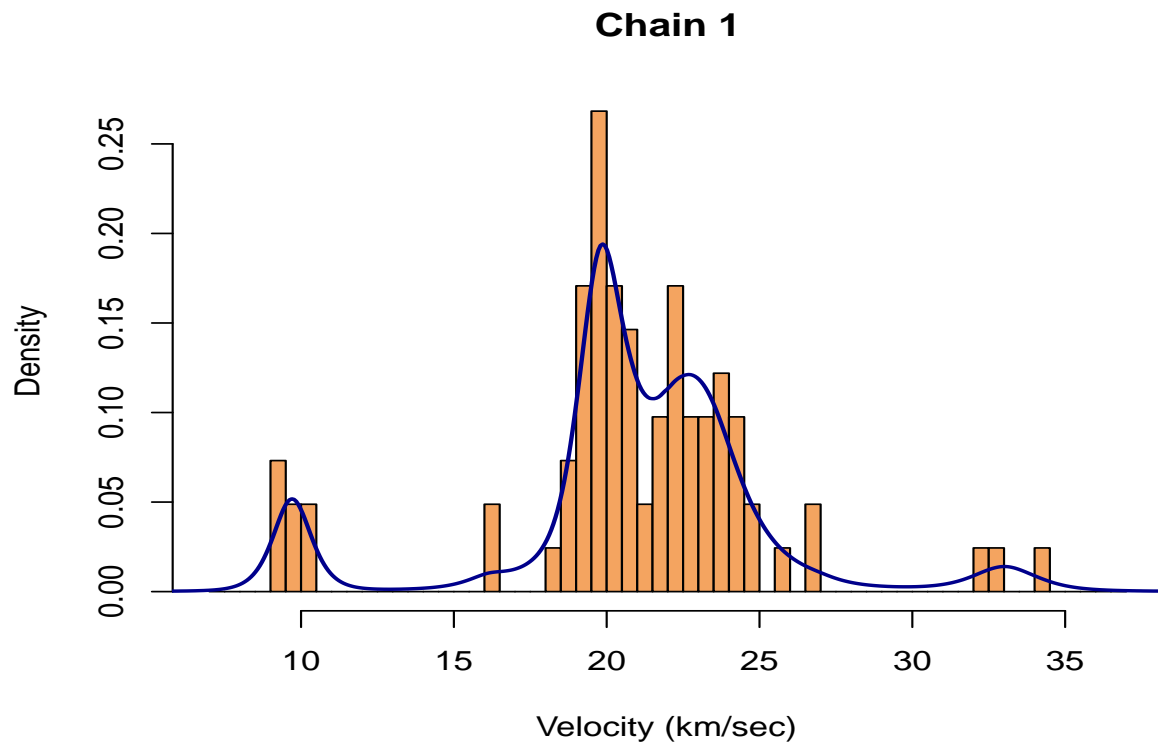


Figure 4: Predictive density (red line) based on the model with a random number of mixture components.

### 4.3 Convergence diagnostics

R⇒ Single chain convergence diagnostics using chain 1 will be shown here.

```
> CH <- 1
```

R⇒ Converting the chains into **mcmc** objects to be used in the package **coda**:

```
> if (RUN.ALLOUT){  
+   start <- RJModel2[[CH]]$nMCMC["burn"] + 1  
+   end <- RJModel2[[CH]]$nMCMC["burn"] + RJModel2[[CH]]$nMCMC["keep"]  
+   chK <- mcmc(RJModel2[[CH]]$K, start=start, end=end)  
+   chgammaInv <- mcmc(RJModel2[[CH]]$gammaInv, start=start, end=end)  
+   chmixture <- mcmc(RJModel2[[CH]]$mixture, start=start, end=end)  
+   chdeviance <- mcmc(RJModel2[[CH]]$deviance, start=start, end=end)  
+ }
```

R⇒ Traceplots for selected parameters (not shown) can be drawn using the following commands:

```
> if (RUN.ALLOUT){  
+   lwd <- 0.5  
+   postscript(paste(FIGKEEPDIR, "figGalaxy07.ps", sep=""), width=6, height=9,  
+             horizontal=FALSE)  
+   par(mfrow=c(2, 2), bty="n")  
+   traceplot(chK, smooth=FALSE, col="darkgreen", lwd=lwd, main="K")  
+   traceplot(chgammaInv[, "gammaInv1"], smooth=FALSE,  
+            col="brown", lwd=lwd, main="gamma^{-1}")  
+   traceplot(chmixture[, "y.Mean.1"], smooth=FALSE,  
+            col="darkblue", lwd=lwd, main="EY")  
+   traceplot(chmixture[, "y.SD.1"], smooth=FALSE,  
+            col="darkblue", lwd=lwd, main="sd(Y)")  
+   dev.off()  
+ #  
+   postscript(paste(FIGKEEPDIR, "figGalaxy08.ps", sep=""), width=6, height=9,  
+             horizontal=FALSE)  
+   par(mfrow=c(2, 2), bty="n")  
+   traceplot(chdeviance[, "LogL0"], smooth=FALSE,  
+            col="red", lwd=lwd, main="Log(L0)")  
+   traceplot(chdeviance[, "LogL1"], smooth=FALSE,  
+            col="red", lwd=lwd, main="Log(L1)")  
+   traceplot(chdeviance[, "dev.complete"], smooth=FALSE,  
+            col="red", lwd=lwd, main="D(complete)")  
+   traceplot(chdeviance[, "dev.observed"], smooth=FALSE,  
+            col="red", lwd=lwd, main="D(observed)")  
+   dev.off()  
+ }
```

R⇒ On Figure 5, we show a traceplot of  $K$  of last 10 000 iterations drawn using the following commands:

```
> if (RUN.ALLOUT){
+   chKpart <- mcmc(RJModel2[[CH]]$K[490001:500000], start=start+490000, end=end)
+   postscript(paste(FIGKEEPDIR, "figGalaxy07a.ps", sep=""), width=9, height=6,
+             horizontal=FALSE)
+   par(mfrow=c(1, 1), bty="n")
+   traceplot(chKpart, smooth=FALSE, col="darkgreen", main="K")
+   dev.off()
+ }
```

R⇒ Posterior density estimates for selected parameters (see Figure 6):

```
> if (RUN.ALLOUT){
+   postscript(paste(FIGKEEPDIR, "figGalaxy09.ps", sep=""), width=6, height=9,
+             horizontal=FALSE)
+   par(mfrow=c(2, 2), bty="n")
+   densplot(chK, show.obs=FALSE, col="darkgreen", main="K")
+   densplot(chgammaInv[, "gammaInv1"], show.obs=FALSE,
+            col="brown", main="gamma-1", xlim=c(0, 30))
+   densplot(chmixture[, "y.Mean.1"], show.obs=FALSE,
+            col="darkblue", main="EY", xlim=c(15, 25))
+   densplot(chmixture[, "y.SD.1"], show.obs=FALSE,
+            col="darkblue", main="sd(Y)", xlim=c(0, 12))
+   dev.off()
+ }
```

R⇒ Autocorrelation plots for selected parameters (see Figure 7):

```
> if (RUN.ALLOUT){
+   postscript(paste(FIGKEEPDIR, "figGalaxy10.ps", sep=""), width=6, height=9,
+             horizontal=FALSE)
+   par(mfrow=c(2, 2), bty="n")
+   autocorr.plot(chK, auto.layout=FALSE, ask=FALSE,
+                 col="darkgreen", lwd=2, main="K")
+   autocorr.plot(chgammaInv[, "gammaInv1"], auto.layout=FALSE, ask=FALSE,
+                 col="brown", lwd=2, main="gamma-1")
+   autocorr.plot(chmixture[, "y.Mean.1"], auto.layout=FALSE, ask=FALSE,
+                 col="darkblue", lwd=2, main="EY")
+   autocorr.plot(chmixture[, "y.SD.1"], auto.layout=FALSE, ask=FALSE,
+                 col="darkblue", lwd=2, main="sd(Y)")
+   dev.off()
+ }
```

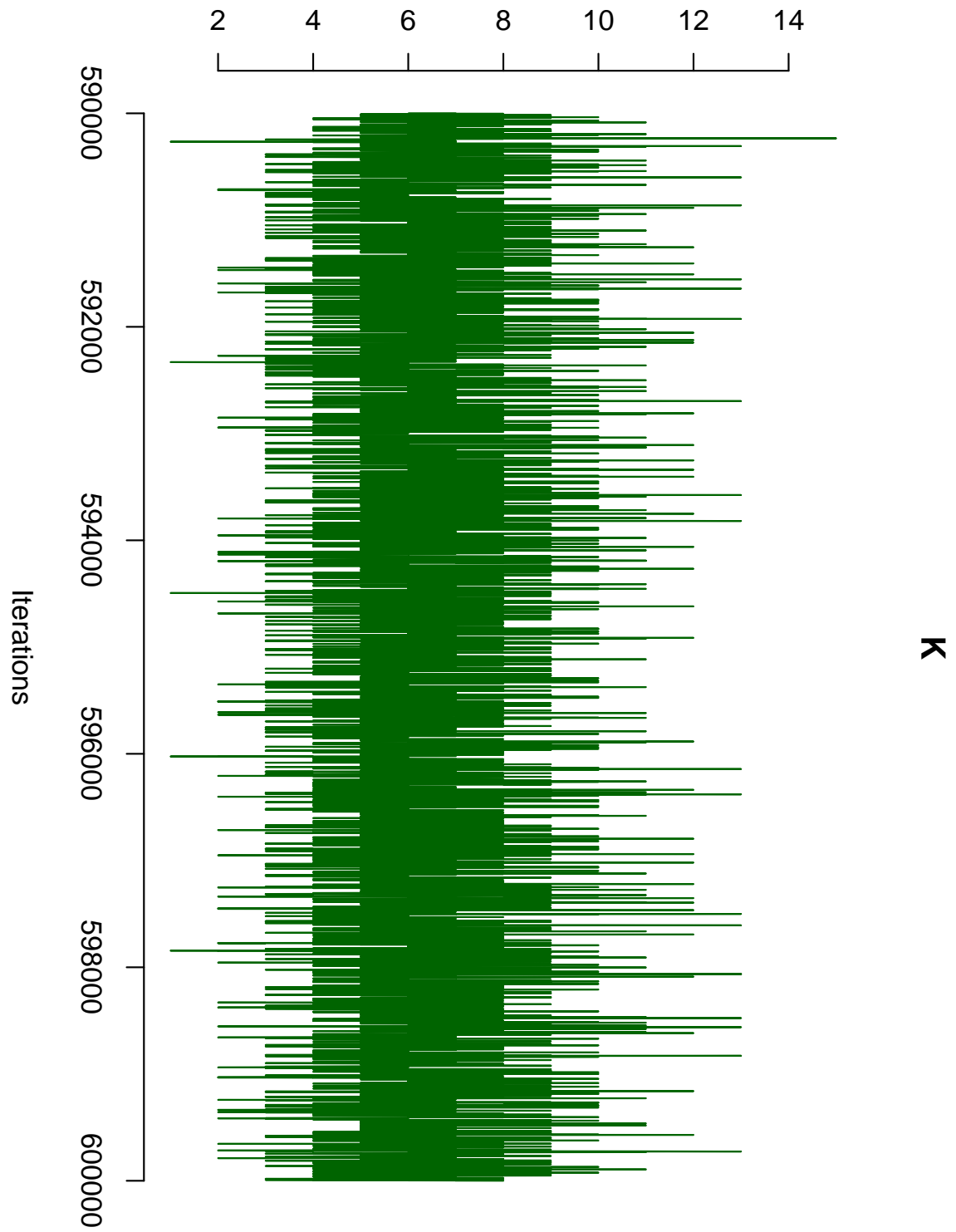


Figure 5: Model with a random number of mixture components. Traceplots for the number of mixture components  $K$  (last 10 000 iterations).

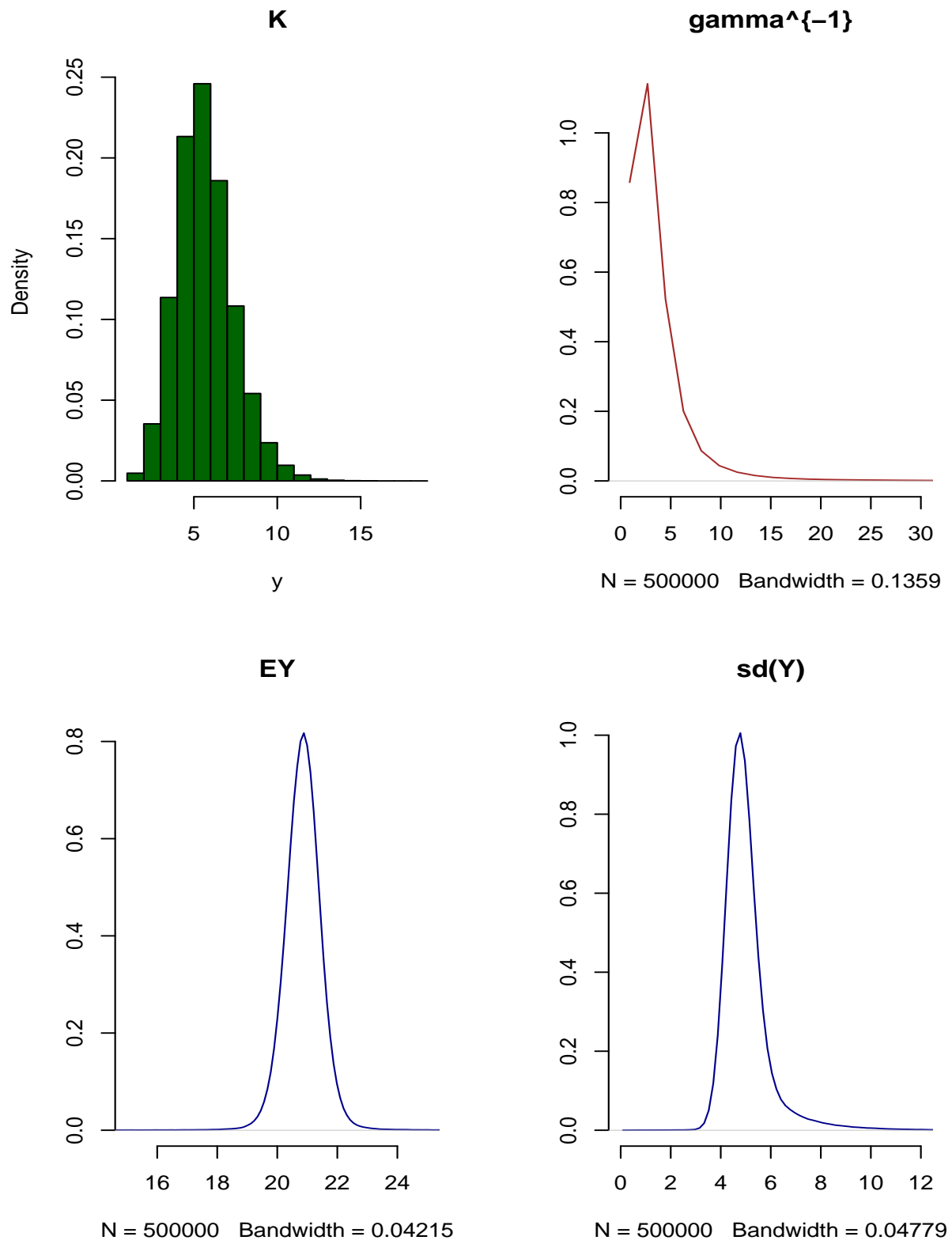


Figure 6: Model with a random number of mixture components. Posterior density estimates for selected parameters.

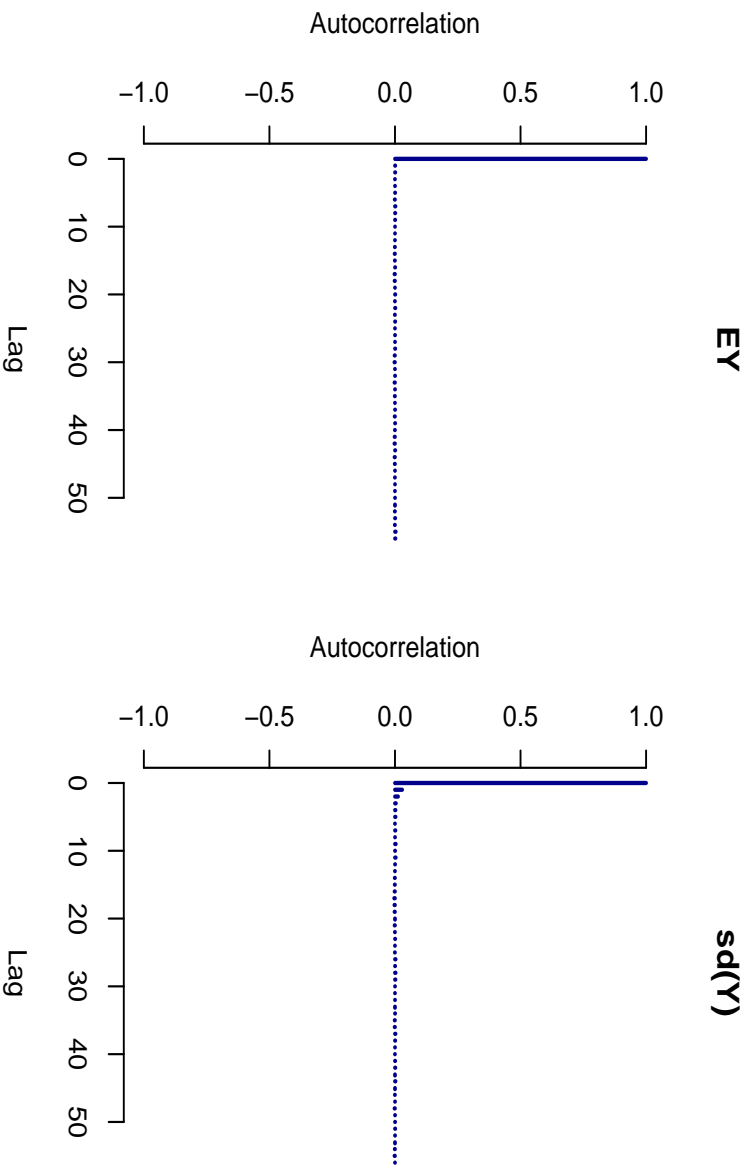
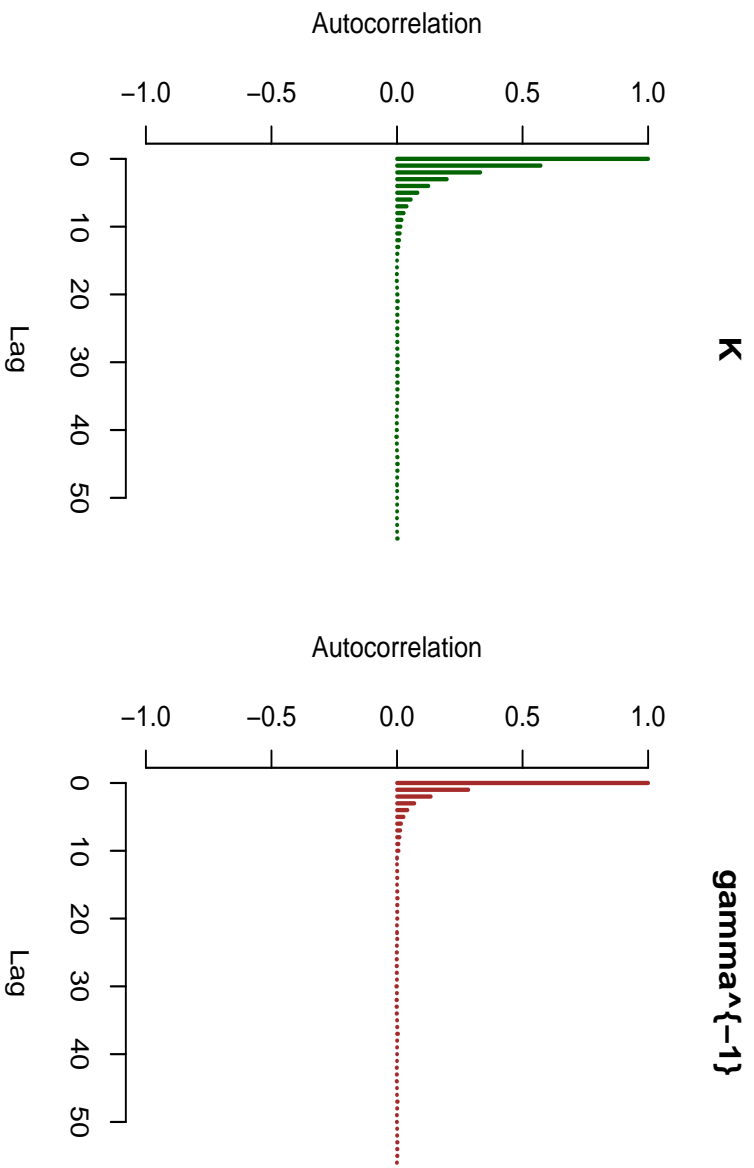


Figure 7: Model with a random number of mixture components. Autocorrelation plots for selected parameters.

## 5 Model with a fixed number of components

We will fit a mixture model for  $K = 1, \dots, 10$ , compare the deviance based quantities and predictive densities. For the prior hyperparameters common to the model with a random  $K$ , we will use the same as in the model [RJModel2](#).

R⇒ Specification of the prior hyperparameters:

```
> FixPrior2 <- list(priorK="fixed",
+                   delta=1,
+                   priormuQ="independentC", xi=21.73, D=630.5121,
+                   zeta=2*2, g=0.2, h=0.016/2)
```

R⇒ Running the MCMC simulation for  $K = 1, \dots, 10$  (output printed during the MCMC run on the screen not shown), computation of predictive densities.

R⇒ After predictive densities are computed, we remove all chains from resulting objects (to save some memory).

```
> if (RUN.TIMECONSUMING.CODE){
+   Keep <- c("iter", "nMCMC", "dim", "prior", "init", "RJMCMC",
+           "scale", "state", "freqK", "propK", "DIC", "moves",
+           "pm.y", "pm.z", "pm.indDev", "pred.dens", "summ.y.Mean",
+           "summ.y.SDCorr", "summ.z.Mean", "summ.z.SDCorr")
+   set.seed(770328)
+   FixModel2 <- list()
+   PDensFix2 <- list()
+   for (k in 1:10){
+     cat(paste("K = ", k, "\n-----\n", sep=""))
+     PriorNow <- FixPrior2
+     PriorNow$Kmax <- k
+     FixModel2[[k]] <- NMixMCMC(y0=Galaxy, prior=PriorNow, nMCMC=nMCMC,
+                               scale=list(shift=0, scale=1), PED=TRUE)
+     #
+     cat(paste("\nComputation of pred. densities started on ", date(),
+               "\n", sep=""))
+     PDensFix2[[k]] <- list()
+     PDensFix2[[k]][[1]] <- NMixPredDensMarg(FixModel2[[k]][[1]], grid=ygrid)
+     PDensFix2[[k]][[2]] <- NMixPredDensMarg(FixModel2[[k]][[2]], grid=ygrid)
+     cat(paste("Computation of pred. densities finished on ", date(),
+               "\n\n\n", sep=""))
+     #
+     FixModel2[[k]][[1]] <- FixModel2[[k]][[1]][Keep]
+     FixModel2[[k]][[2]] <- FixModel2[[k]][[2]][Keep]
+     class(FixModel2[[k]][[1]]) <- class(FixModel2[[k]][[2]]) <- "NMixMCMC"
+   }
+ }
```



R⇒ Basic posterior summary of the fitted model with  $K = 6$ :

```
> print(FixModel2[[6]])
```

```
6 component normal mixture estimated using MCMC
=====
```

Penalized expected deviance:

```
-----
D.expect  p(opt)      PED  wp(opt)    wPED
427.1929  118.7859  545.9789  136.7527  563.9456
```

Deviance information criteria:

```
-----
          DIC          pD      D.bar D.in.bar
Chain 1  449.0657  26.08602  422.9797  396.8936
Chain 2  448.5626  25.84903  422.7136  396.8646
```

Posterior summary statistics for moments of mixture for original data:

-----  
Mean:

	Mean	Std.Dev.	Min.	2.5%	1st Qu.	Median	3rd Qu.
Chain 1	20.85548	0.5750815	12.53002	19.71908	20.49663	20.85971	21.21807
Chain 2	20.85448	0.5738582	14.46291	19.71958	20.49497	20.85916	21.21748
	97.5%	Max.					
Chain 1	21.97278	26.53756					
Chain 2	21.96561	27.18524					

Standard deviation:

	Mean	Std.Dev.	Min.	2.5%	1st Qu.	Median	3rd Qu.
Chain 1	4.974256	0.9143447	0.4844963	3.812832	4.467038	4.840967	5.264126
Chain 2	4.969868	0.9081553	0.5223116	3.816097	4.466204	4.839025	5.262335
	97.5%	Max.					
Chain 1	7.254569	33.55014					
Chain 2	7.216001	32.82954					

R⇒ Summary of PED and DIC's for the fitted models:

```
> PED <- RJModel2$PED
> DIC <- list(Chain1 = RJModel2[[1]]$DIC, Chain2 = RJModel2[[2]]$DIC)
> for (k in 1:length(FixModel2)) {
+   PED <- rbind(PED, FixModel2[[k]]$PED)
+   DIC[[1]] <- rbind(DIC[[1]], FixModel2[[k]][[1]]$DIC)
+   DIC[[2]] <- rbind(DIC[[2]], FixModel2[[k]][[2]]$DIC)
+ }
> rownames(PED) <- rownames(DIC[[1]]) <- rownames(DIC[[2]]) <- c("RJ-MCMC",
+   paste("K = ", 1:length(FixModel2), sep = ""))
```

```
> print(PED)
```

	D.expect	p(opt)	PED	wp(opt)	wPED
RJ-MCMC	423.0743	114.340974	537.4152	126.374978	549.4492
K = 1	482.8301	4.070529	486.9006	4.087999	486.9181
K = 2	446.1402	11.436937	457.5771	11.845757	457.9859
K = 3	418.7662	20.787964	439.5542	20.947999	439.7142
K = 4	418.9034	42.658219	461.5616	50.636206	469.5396
K = 5	422.9906	73.942819	496.9334	88.074453	511.0651
K = 6	427.1929	118.785942	545.9789	136.752672	563.9456
K = 7	430.2111	169.979802	600.1909	190.077819	620.2889
K = 8	430.2424	223.377508	653.6199	242.123948	672.3664
K = 9	431.0306	283.241647	714.2723	300.760083	731.7907
K = 10	430.5812	345.667178	776.2484	360.986272	791.5675

```
> print(DIC)
```

```
$Chain1
```

	DIC	pD	D.bar	D.in.bar
RJ-MCMC	442.6806	22.232147	420.4485	398.2163
K = 1	485.7709	2.944780	482.8261	479.8813
K = 2	451.1053	4.975623	446.1297	441.1540
K = 3	424.3881	5.633584	418.7545	413.1209
K = 4	430.7262	13.770323	416.9559	403.1856
K = 5	440.3760	20.656563	419.7195	399.0629
K = 6	449.0657	26.086023	422.9797	396.8936
K = 7	455.5718	30.243397	425.3284	395.0850
K = 8	457.5007	32.272065	425.2286	392.9565
K = 9	461.5795	35.464813	426.1146	390.6498
K = 10	463.4231	37.683232	425.7399	388.0567

```
$Chain2
```

	DIC	pD	D.bar	D.in.bar
RJ-MCMC	442.6908	22.221437	420.4693	398.2479
K = 1	485.7925	2.958353	482.8341	479.8758
K = 2	451.7327	5.582011	446.1507	440.5686
K = 3	424.4238	5.645818	418.7779	413.1321
K = 4	431.3099	14.069949	417.2400	403.1700
K = 5	441.2720	21.105927	420.1661	399.0602
K = 6	448.5626	25.849028	422.7136	396.8646
K = 7	453.9765	29.467170	424.5093	395.0422
K = 8	457.7424	32.372631	425.3697	392.9971
K = 9	460.9831	35.177570	425.8055	390.6279
K = 10	463.7275	37.841151	425.8863	388.0452

R⇒ Plot of the predictive densities for different values of  $K$  based on chain 1 (see Figures 8 and 9):

```
> postscript(paste(FIGDIR, "figGalaxy05.ps", sep=""), width=6, height=6,
+           horizontal=FALSE)
> par(mfrow=c(1, 1), bty="n")
> hist(Galaxy, prob=TRUE, col="grey90", breaks=seq(7, 37, by=0.5),
+      xlab="Velocity (km/sec)", ylab="Density", main="")
> for (k in 1:10){
+   lines(PDensFix2[[k]][[1]]$x$x1, PDensFix2[[k]][[1]]$dens[[1]], col="red")
+ }
> dev.off()

> postscript(paste(FIGDIR, "figGalaxy06.ps", sep=""), width=6, height=9,
+           horizontal=FALSE)
> par(mar=c(3, 2, 2, 1)+0.1)
> par(mfrow=c(5, 2), bty="n")
> for (k in 1:10){
+   hist(Galaxy, prob=TRUE, col="lightblue", breaks=seq(7, 37, by=0.5),
+      xlab="", ylab="", main=paste("K = ", k, sep=""))
+   lines(PDensFix2[[k]][[1]]$x$x1, PDensFix2[[k]][[1]]$dens[[1]], col="red", lwd=2)
+ }
> dev.off()
```

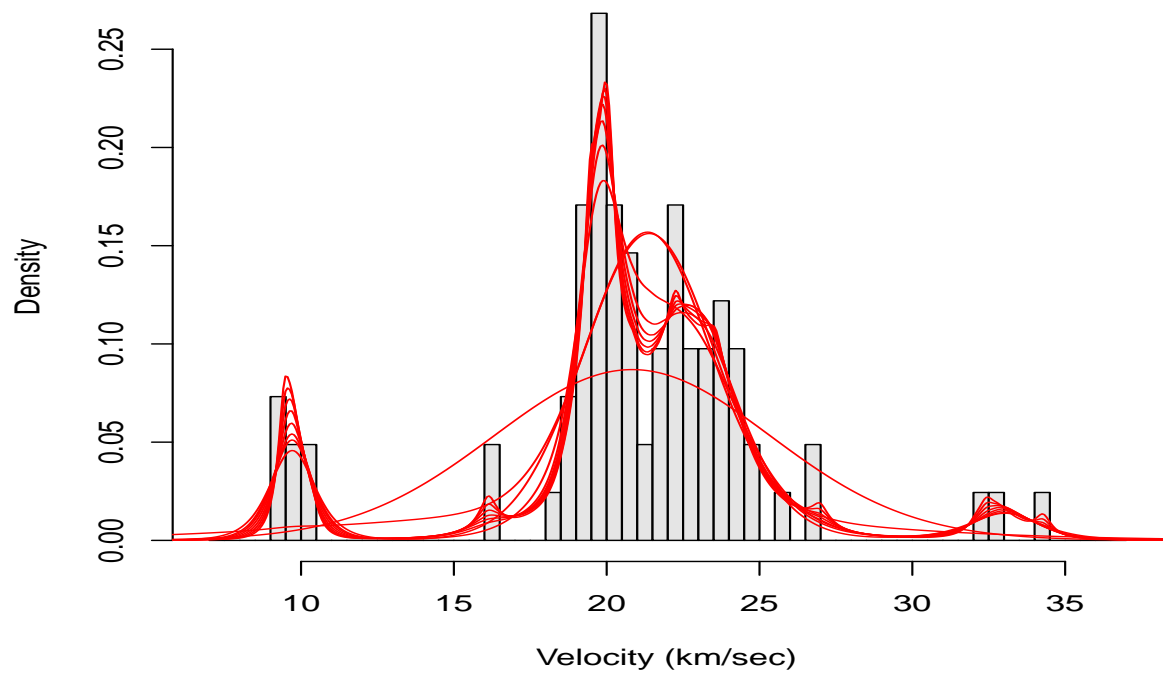


Figure 8: Predictive densities based on the models with a fixed number of mixture components (results from chain 1).

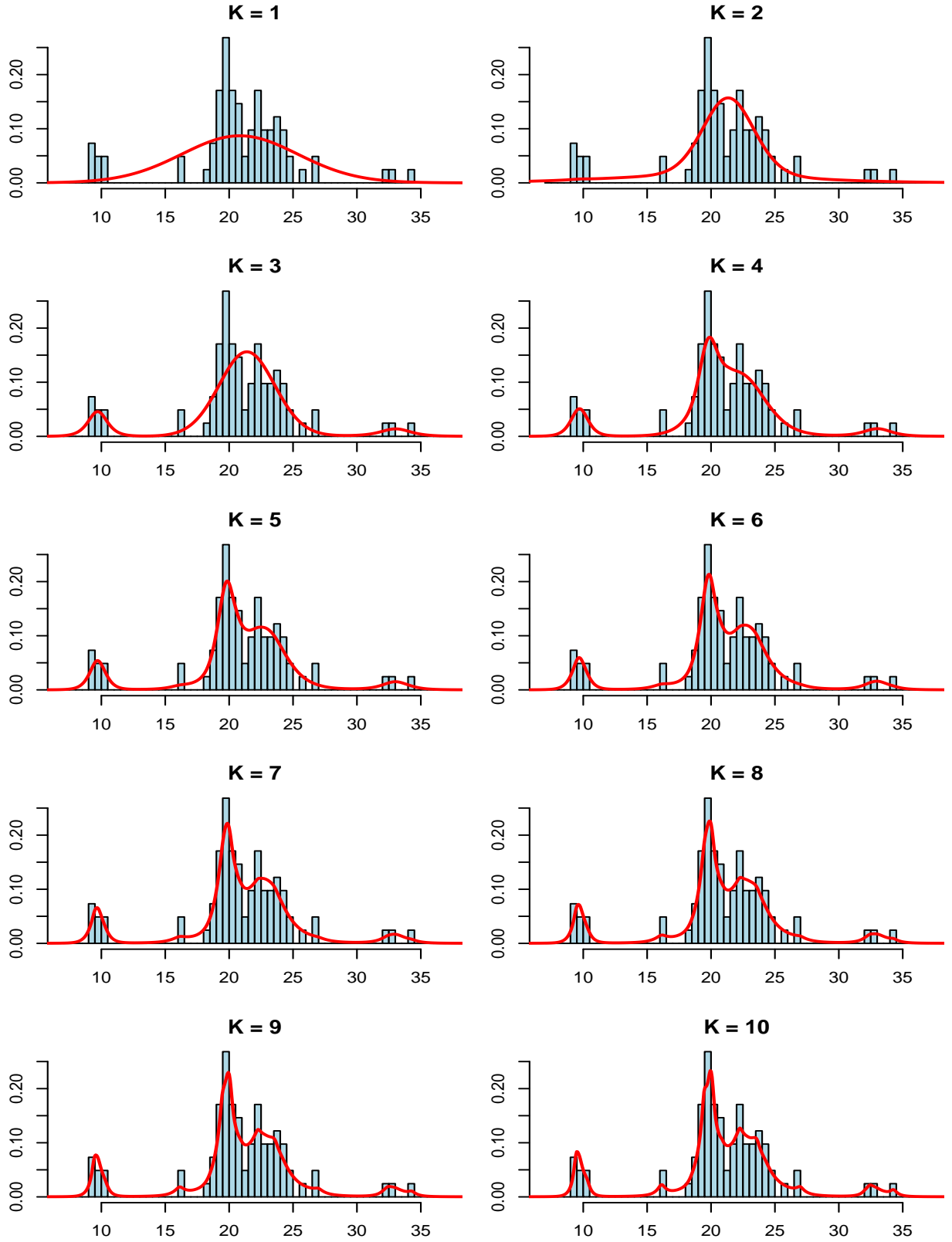


Figure 9: Predictive densities based on the models with a fixed number of mixture components (results from chain 1).

R⇒ Save results for future use. For file Galaxy-Result.RData, we exclude all chains from object RJModel2.

```
> if (RUN.TIMECONSUMING.CODE){  
+   save(list="RJModel2",  
+       file=paste(RESULTDIR, "Galaxy-RJ2.RData", sep=""))  
+  
+   Keep <- c("iter", "nMCMC", "dim", "prior", "init", "RJMCMC",  
+           "scale", "state", "freqK", "propK", "DIC", "moves",  
+           "pm.y", "pm.z", "pm.indDev", "pred.dens", "summ.y.Mean",  
+           "summ.y.SDCorr", "summ.z.Mean", "summ.z.SDCorr")  
+   #  
+   RJModel2[[1]] <- RJModel2[[1]][Keep]  
+   RJModel2[[2]] <- RJModel2[[2]][Keep]  
+   class(RJModel2[[1]]) <- class(RJModel2[[2]]) <- "NMixMCMC"  
+   #  
+   save(list=c("RJModel2", "PDensRJ2", "FixModel2", "PDensFix2"),  
+       file=paste(RESULT2DIR, "/Galaxy-Result.RData", sep=""))  
+ }
```

## References

- KOMÁREK, A. (2009). A new R package for Bayesian estimation of multivariate normal mixtures allowing for selection of the number of components and interval-censored data. *Computational Statistics and Data Analysis*, **53**, To appear.
- RICHARDSON, S. and GREEN, P. J. (1997). On Bayesian analysis of mixtures with unknown number of components (with Discussion). *Journal of the Royal Statistical Society, Series B*, **59**, 731–792.
- ROEDER, K. (1990). Density estimation with confidence sets exemplified by superclusters and voids in the galaxies. *Journal of the American Statistical Association*, **85**, 617–624.