

extremevalues

A package for outlier detection

Version 2.0

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1 Introduction

This package provides the implementation of the outlier detection method as described in van der Loo (2010). Briefly, the method works as follows: given a univariate dataset \mathbf{y} , with values y_1, y_2, \dots, y_N which is assumed to be drawn from a model distribution with cdf $F(Y|\boldsymbol{\theta})$. The package determines which (if any) of the extreme observations y_1, y_2, \dots and/or y_N, y_{N-1} are outliers in two steps:

1. Estimate the distribution's parameters $\hat{\boldsymbol{\theta}}$ by fitting a model cdf F to the QQ plot positions of the bulk of the observed data. The bulk is all data between a minimum and maximum quantile (default: 0.1 and 0.9) which can be set by the user.
2. Determine whether the extreme observations are unlikely to be drawn from $F(Y|\hat{\boldsymbol{\theta}})$. There are two ways of doing this:

Method I: Calculate the limit ℓ_ρ^\pm above (+) or below (−) less than ρ observations are expected, given $F(Y|\hat{\theta})$ and the number of observations N . The observations $y_1, y_2, \dots < \ell_\rho^-$ are left outliers and the observations $y_N, y_{N-1} > \ell_\rho^+$ are right outliers. The value of ρ (default: 1.0) can be set by the user for left and right outliers separately.

Method II: Estimate the $1 - 2\alpha$ confidence interval for the residuals resulting from the fit which determines the model distribution $F(Y|\hat{\theta})$. Label the upper (+) and lower (−) limits of this interval with ℓ_α^\pm . Extreme values which were not used in the fit are left (right) outliers when their residuals are larger negative (larger positive) than ℓ_α^- (ℓ_α^+). The values ℓ_α^\pm are estimated assuming normally distributed residuals and the value of α (default: 0.05) may be set by the user for left and right outliers separately.

The main purpose of the `extremevalues` package is to provide functions which can detect outliers using the methods described above. Additionally, plotfunctions are provided for graphical analysis of the result. The package currently supports four model distributions:

- Lognormal distribution
- Exponential distribution
- Pareto distribution
- Weibull distribution
- Normal distribution

In this document we work through an example to familiarize the reader with the use of the package. I refer to the R help files for a complete description of the functions and to the reference mentioned above for a better explanation of the methodology.

2 A quick example

Generate some lognormally distributed data:

```
> y <- rlnorm(200)
```

(You can probably reconstruct the exact results using `set.seed(123456789)` first, as I did. There might still be differences since the output of pseudorandom generators can depend on the architecture of the machine it's running on.) Let's add a left and a right outlier:

```
> y <- c(y,0.1*min(y),10*max(y))
```

And try to detect them using (the default) Method I.

```
> L <- getOutliers(y, distribution="lognormal")
```

The number of left and right detected outliers are

```
> L$nOut
Left Right
      1    1
```

The position of left and right outliers are stored as indices:

```
> L$iLeft
[1] 201
```

```
> L$iRight
[1] 202
```

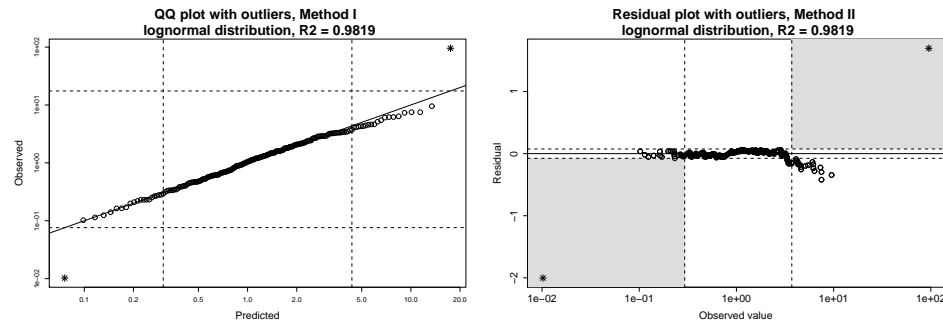
Now, let's use Method II:

```
M <- getOutliers(y,distribution="lognormal", method="II")
```

To see what we have done, we can plot the results with:

```
> par(mfrow=c(1,2))
> outlierPlot(y,L)
> outlierPlot(y,M,mode="residual")
```

The resulting picture looks something like this:



The left panel shows a QQ plot for y based on the lognormal distribution. The values between the vertical dotted lines are used in to fit the distribution. Horizontal dotted lines indicate values $\ell_{\rho=1.0}^{\pm}$ above or below which observations are identified as outliers. The outliers are indicated with a *.

The right panel shows a residual plot, based on the fit of the lognormal cdf to the QQ plot positions. Points between vertical lines correspond to data used in the fit. The horizontal lines indicate the outlier limits $\ell_{\alpha=0.05}^{\pm}$. Outliers can only occur in the grey areas and are indicated with a *.

Note. The plots resulting on your screen after copying the code above will have different font sizes and line widths from the figure above. You can get the larger fonts and linewidths by using the `fat=TRUE` option in the plot commands. (but don't use `par(mfrow=c(2,1))` in that case).

3 Version history and list of changes

Version history	
Version	Uploaded
version 1.0	03.12.2009
version 2.0	xx.01.2010

3.1 Important changes in version 2.0

- Added automatic left outlier detection.
- Changed standard value of ρ (Method I)
- Added Method II
- Renaming main functions
- Revised and extended plotting capabilities
- Minor revisions of helpfiles
- Changed equation for calculation of plot positions (after reading paper of Makkonen (2008)).

4 Function listing

User functions

getOutliers	Detect outliers, wrapper.
getOutliersI	idem, using Method I
getOutliersII	idem, using Method II
outlierPlot	Plot detection results, wrapper
qqFitPlot	plot results, Method I
plotMethodII	plot results, Method II
rpareto	Draw from pareto distribution
dpareto	Pareto density function
qpareto	Pareto quantile function
invErf	Inverse error function

Internal functions

fitPareto	Fit data to cumulative pareto distribution
fitLognormal	Fit data to cumulative lognormal distribution
fitExponential	Fit data to cumulative exponential distribution
fitWeibull	Fit data to cumulative weibull distribution
fitNormal	Fit data to cumulative normal distribution
(get/qq)ParetoLimit	Determine outlier limit assuming pareto distribution
(get/qq)LognormalLimit	Determine outlier limit assuming lognormal distribution
(get/qq)ExponentialLimit	Determine outlier limit assuming exponential distribution
(get/qq)WeibullLimit	Determine outlier limit assuming weibull distribution
(get/qq)NormalLimit	Determine outlier limit assuming normal distribution

References

- L. Makkonen. Bringing closure to the plotting position controversy. *Communications in Statistics*, 37:460–467, 2008.
- M. P. J. van der Loo. Model based outlier detection. Technical Report 10xxx, Statistics Netherlands, The Hague, 2010.